

PT-symmetric photonics: hidden reefs on the route toward practical applications

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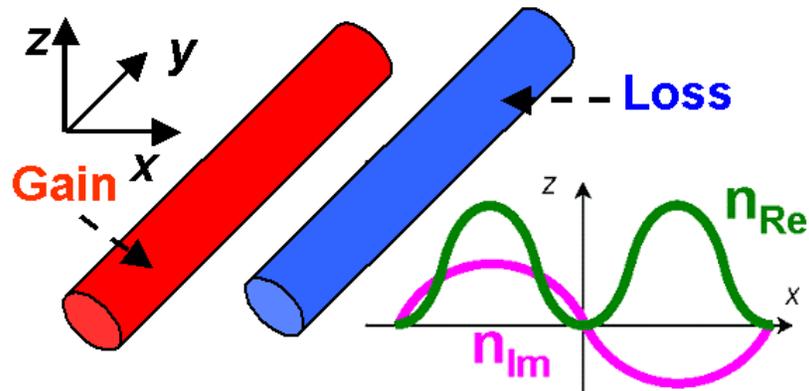
⁴ DTU Fotonik – Technical University of Denmark, Lyngby, Denmark

Outline

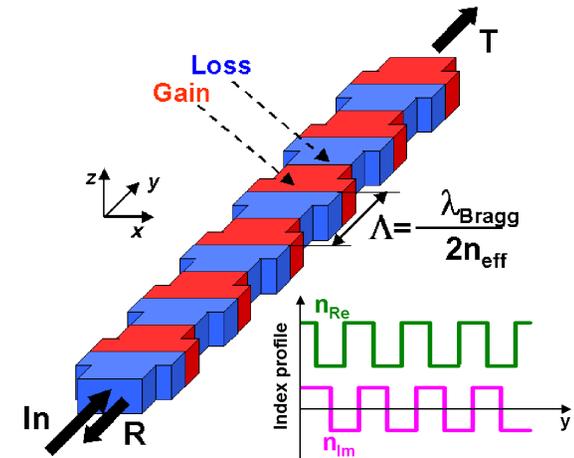
- **Using PT-symmetry for switching applications**
- **Locally PT-symmetric Bragg gratings**
- **PT-symmetry: a new platform for active optical devices**
- **Summary and conclusions**

Parity-Time symmetry in photonics functionalities

PT-symmetric directional coupler



PT-symmetric Bragg grating



PT-symmetry genuine feature:

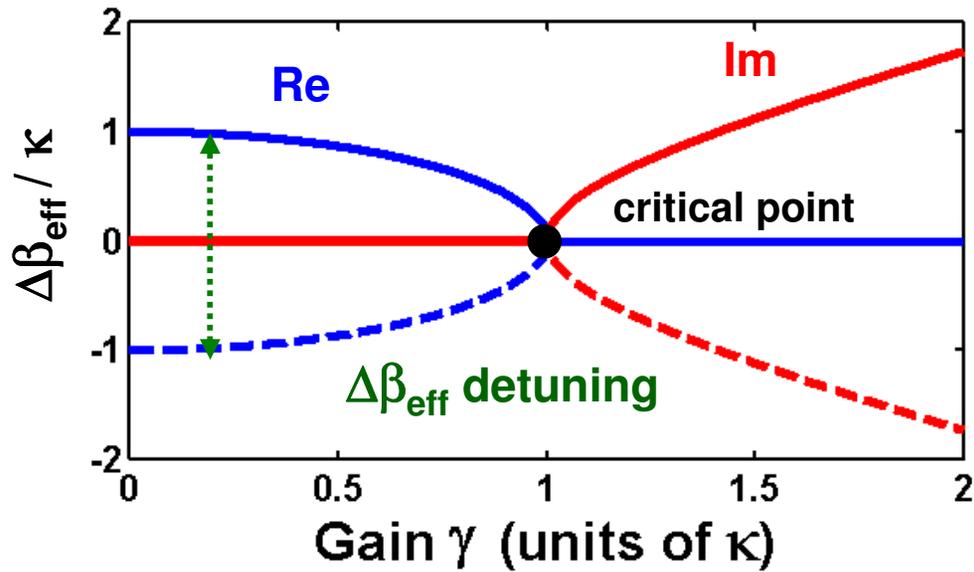
- Functional role of losses

Gain-loss modulated PT-symmetric structures functionalities :

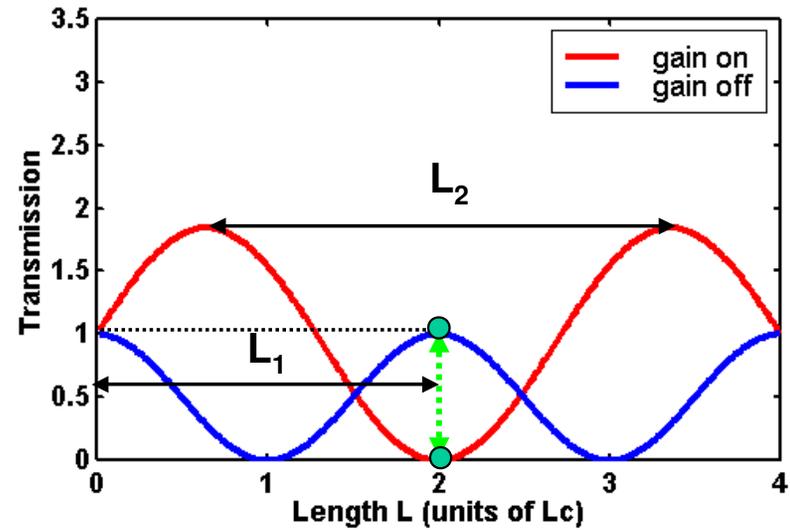
- Switching and tunability
- Spatial (modal) non-reciprocity
- Active tailoring of the grating spectral response and dispersion

Gain-loss modulation electro-optical switching

PT coupled WGs detuning variation

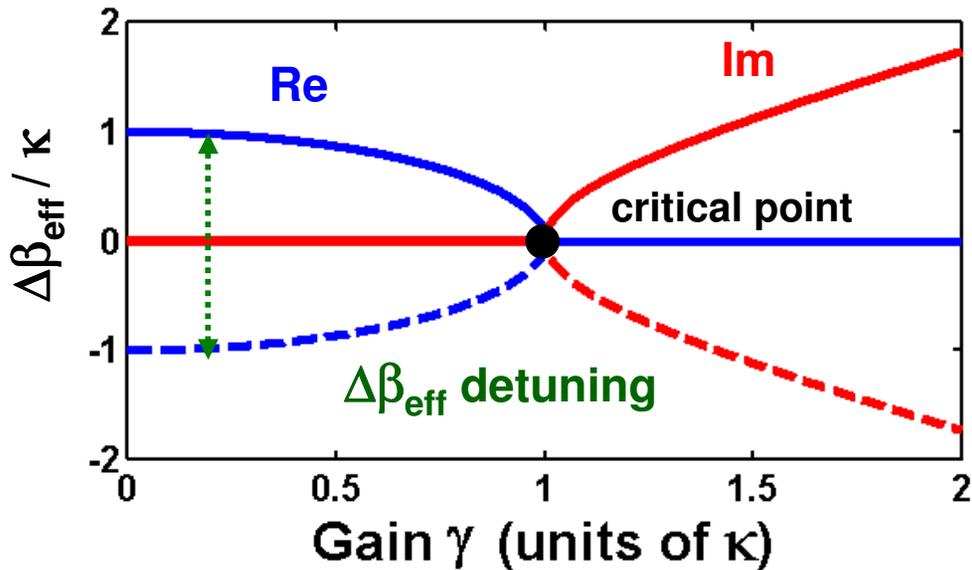


Transmission variation

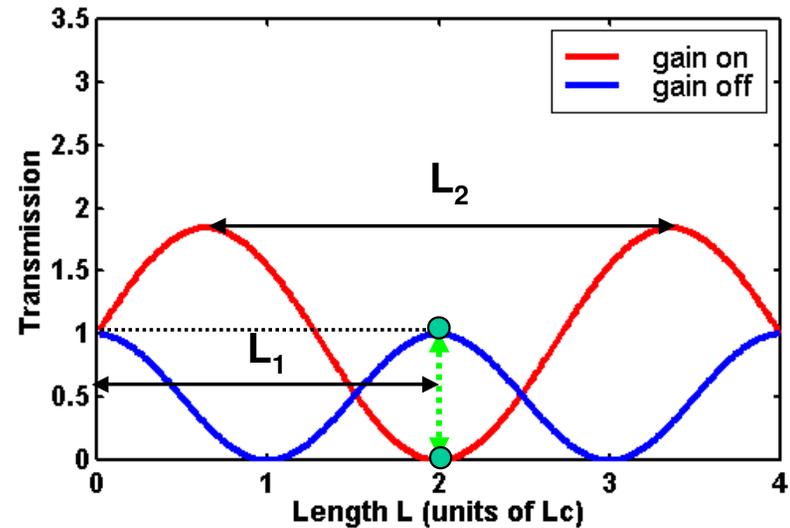


Gain-loss modulation electro-optical switching

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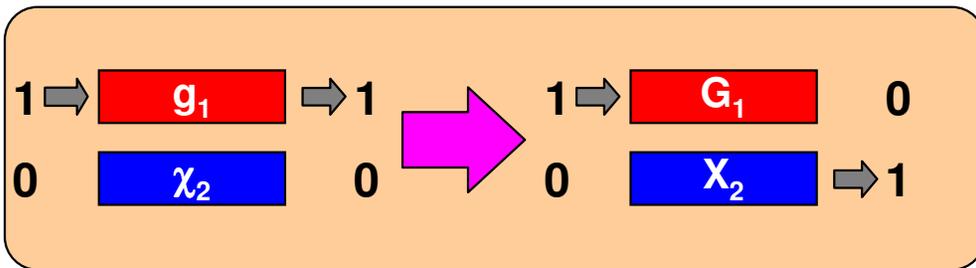


Transmission variation

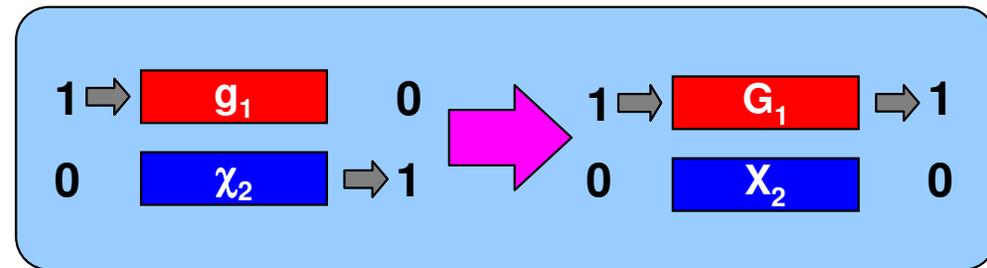


Binary switching operation

Bar \rightarrow Cross: $T_{11}=1, T_{12}=0 \rightarrow T_{11}=0, T_{12}=1$

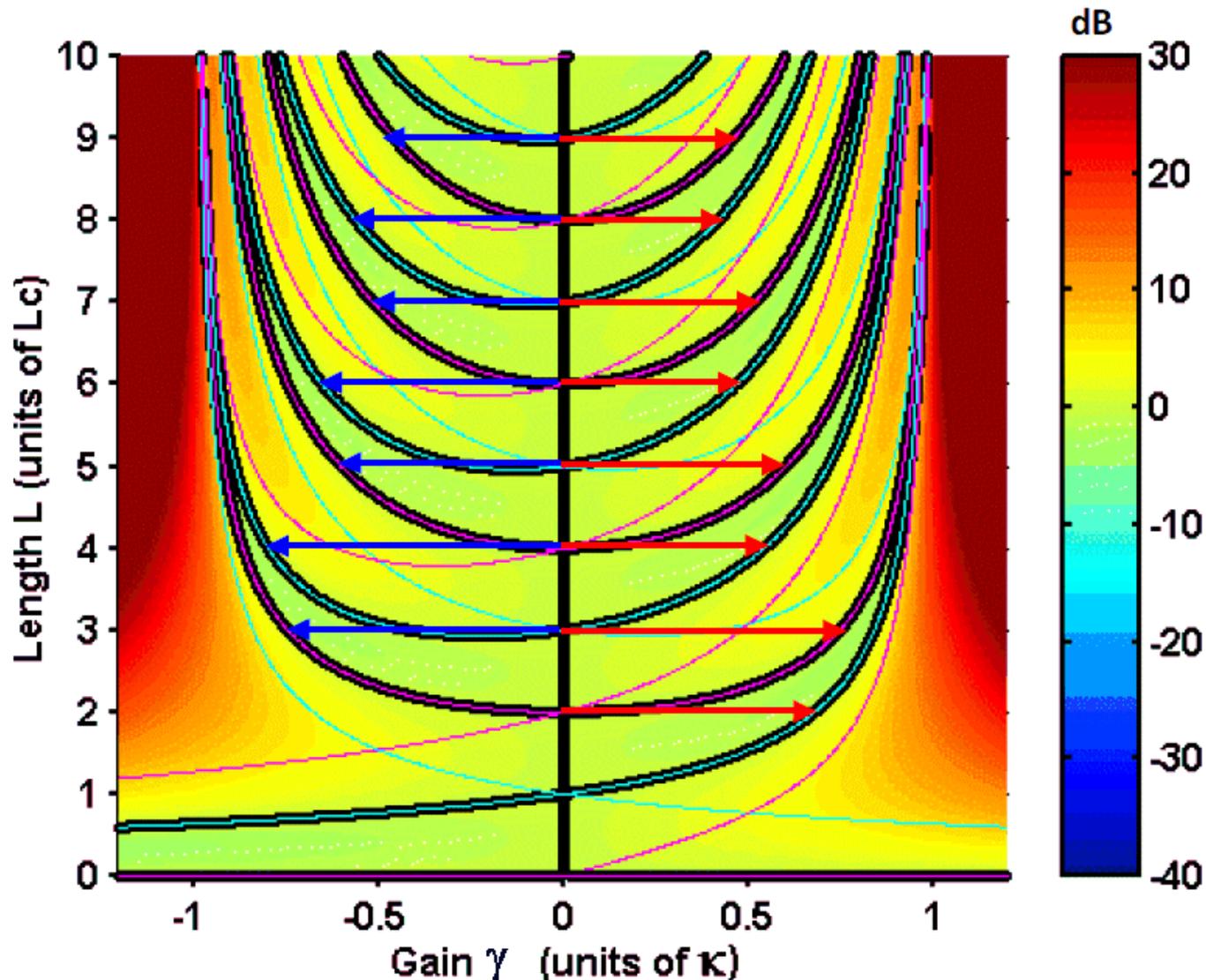


Cross \rightarrow Bar: $T_{11}=1, T_{12}=0 \rightarrow T_{11}=0, T_{12}=1$



Can we obtain binary switching in a non conservative layout?

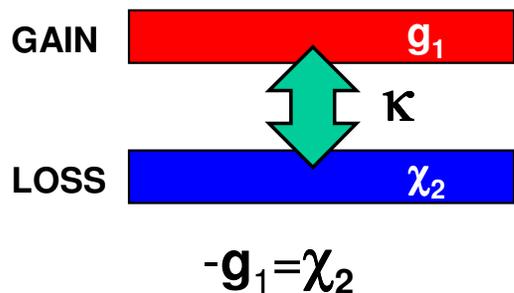
Binary switching in a uniform PT-symmetric coupler



— $T_{11} = 1$ (bar) — $T_{12} = 0$ (cross) — $T_{11} + T_{12} = 1$ (energy conservative states)

What is the minimal gain \times length product for switching?

Control parameter: The imaginary detuning $-\Delta_{im}$



Detuning

$$\delta = \frac{\beta_1 + ig_1 - (\beta_2 - i\chi_2)}{2} = \frac{\beta_1 - \beta_2}{2} + i\Delta_{im}$$

$$\Delta_{im} = \frac{g_1 + \chi_2}{2}$$

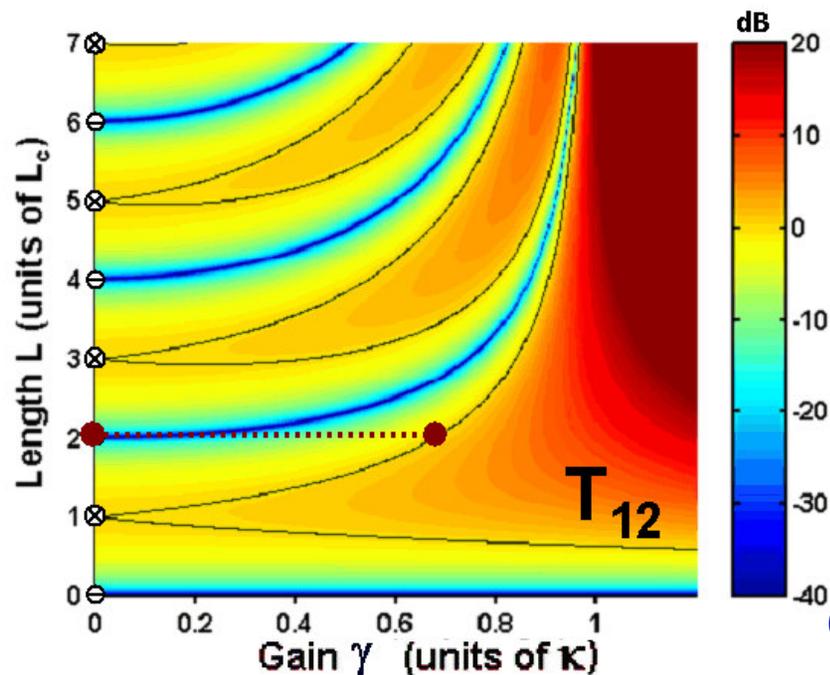
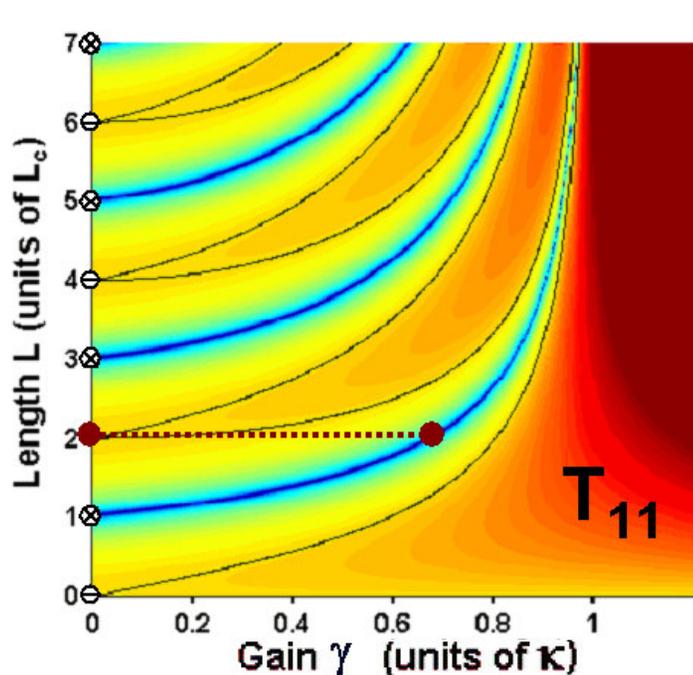
Δ_{im} = imaginary detuning !

A. Lupu, H. Benisty, et al, Opt. Exp. 2013

CMT solution

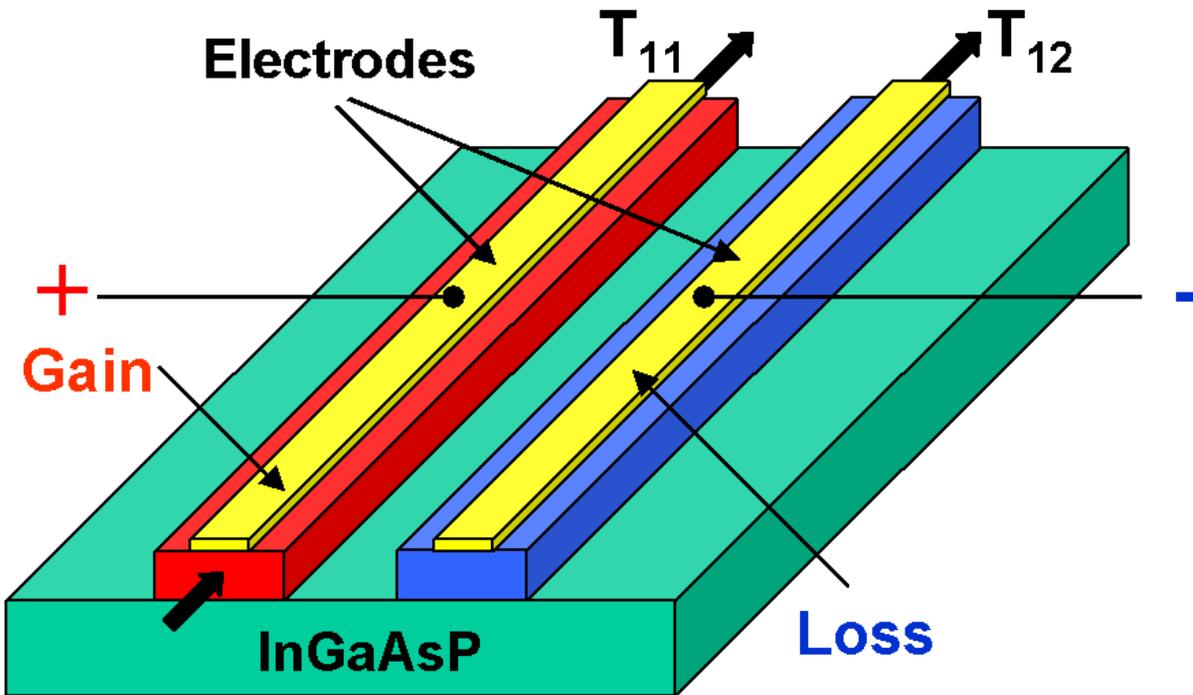
$$\tan\left(\sqrt{\pi^2 - \Delta_{im}^2 L^2}\right) = -\sqrt{\frac{\pi^2}{\Delta_{im}^2 L^2} - 1}$$

$$\Delta_{im} L = \frac{g_1 + \chi_2}{2} 2L_c \approx 0.67\pi \quad \longleftrightarrow \quad 18.6\text{dB}$$



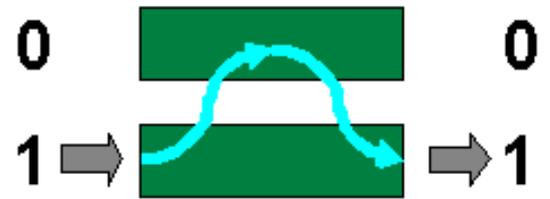
PT-symmetric switch using gain-loss modulation

III-V technology electro-optical switch

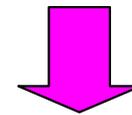


Operation principle

Passive coupler



Bar state



PT coupler



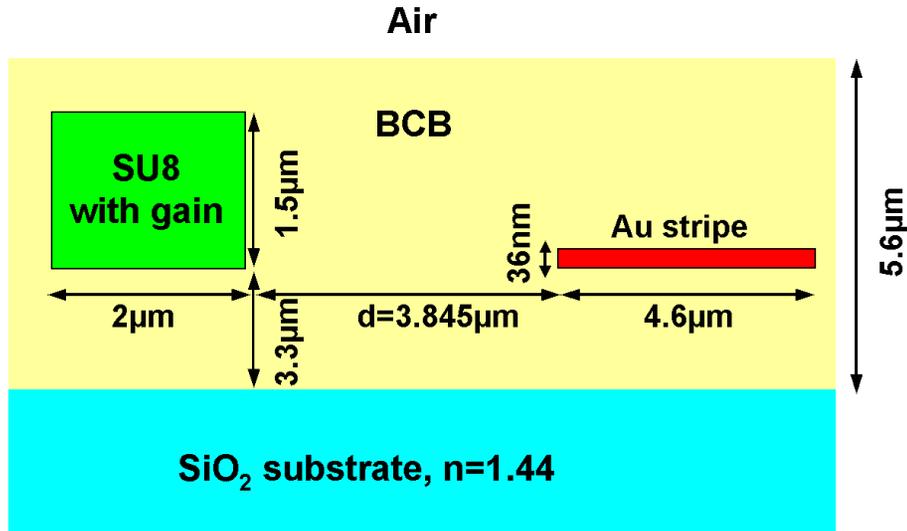
Cross state

Advantages :

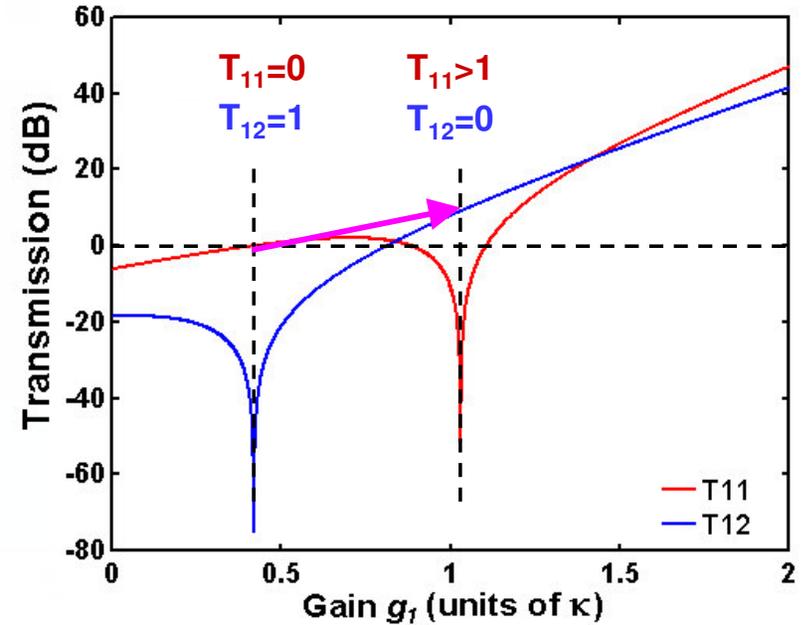
- Compatibility with III-V laser sources fabrication technology
- Emulation of electro-refractive index variation in plasmonics and metamaterials

Impact of material limitations: PTSS with fixed losses

Hybrid plasmonic/dielectric PTSS design

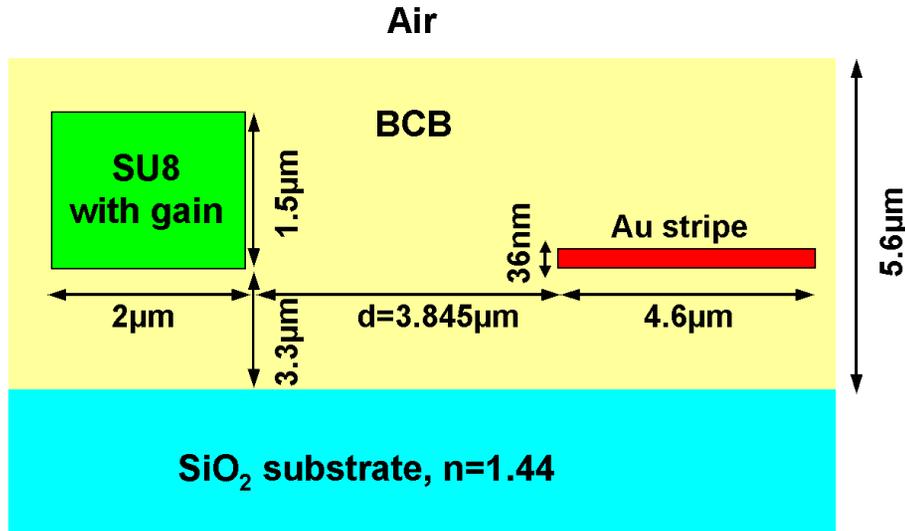


Fixed losses switching operation

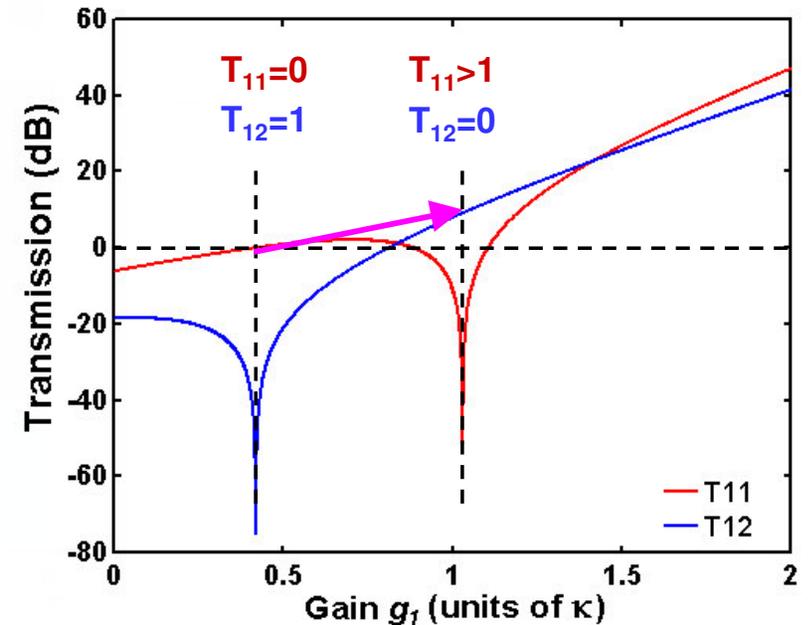


Impact of material limitations: PTSS with fixed losses

Hybrid plasmonic/dielectric PTSS design



Fixed losses switching operation



Coupled modes equations

$$i \frac{\partial}{\partial z} \psi = \begin{pmatrix} \beta + ig & \kappa \\ \kappa & \beta - i\chi \end{pmatrix} \psi$$

↑ gain ↑ losses

Transfer matrix

$$M(z) = \begin{pmatrix} \cos(\Omega z) - \frac{i\delta}{\Omega} \sin(\Omega z) & \frac{i\kappa}{\Omega} \sin(\Omega z) \\ \frac{i\kappa}{\Omega} \sin(\Omega z) & \cos(\Omega z) + \frac{i\delta}{\Omega} \sin(\Omega z) \end{pmatrix}$$

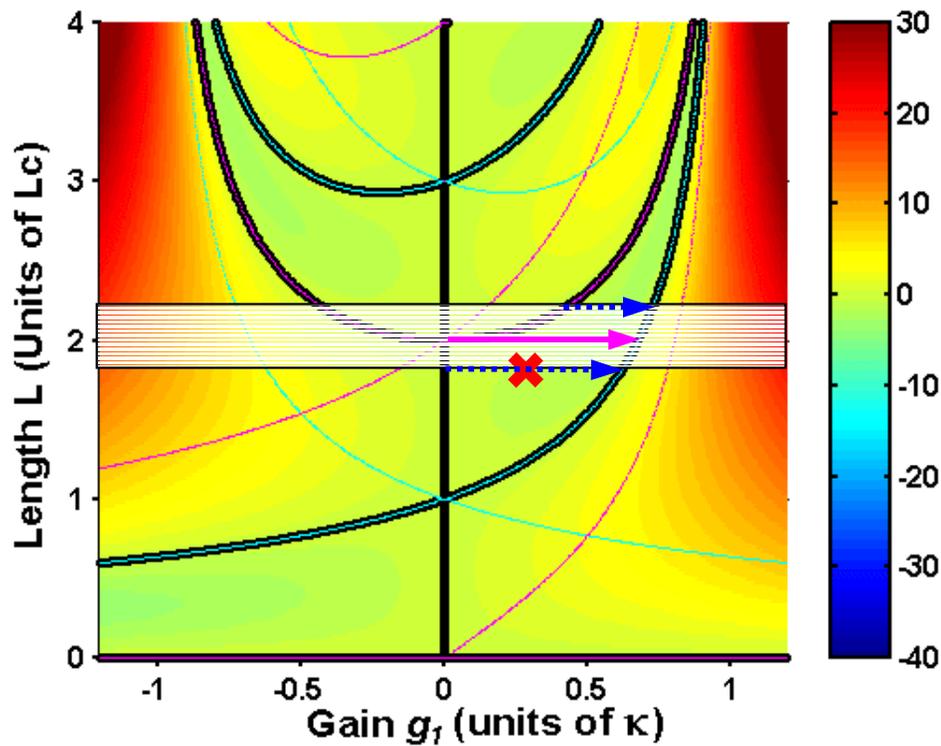
Gauge transformation

$$\exp\left(\frac{g_1 - \chi_2}{2} z\right)$$

Gauge transformation doesn't affect the zeros of PTSS !

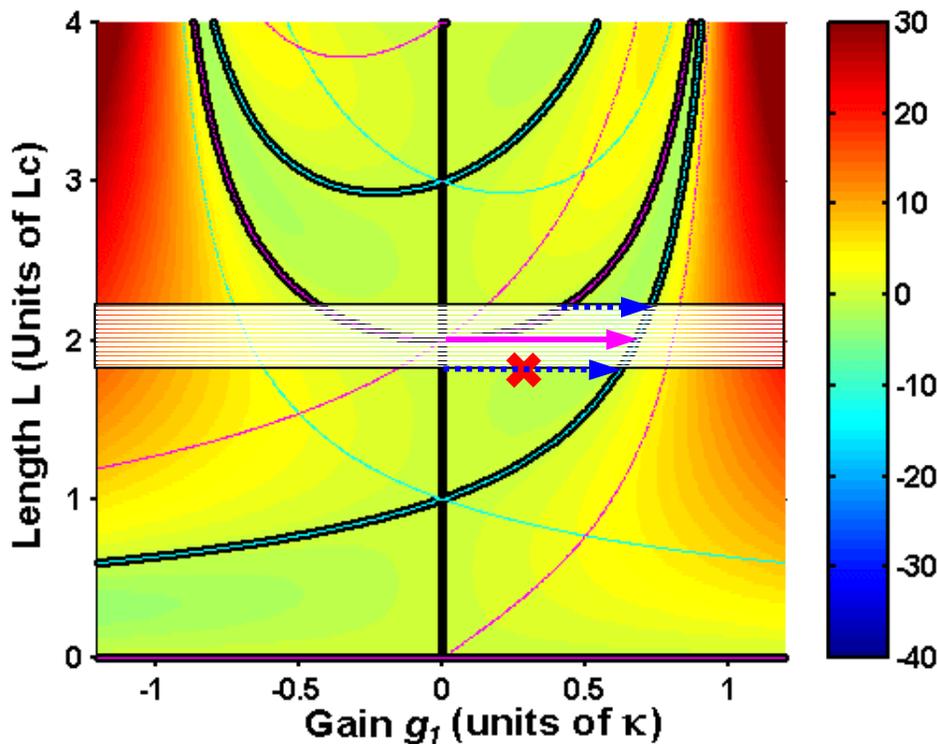
Impact of technological imperfections: deviation from the nominal coupling length

Nominal coupling length $L=2L_c$

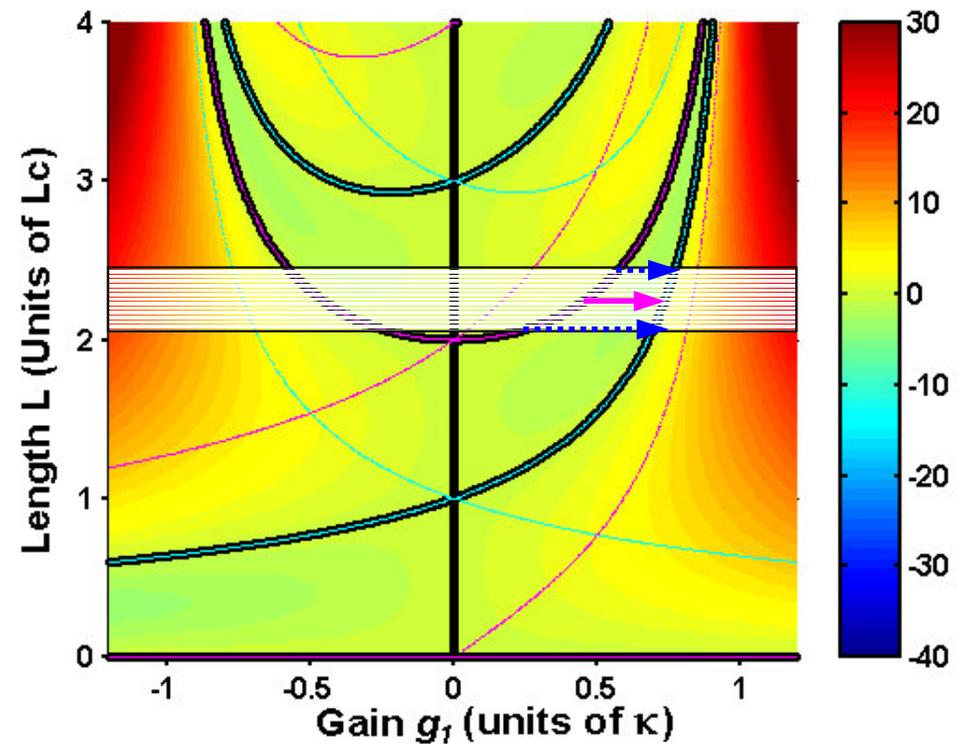


Impact of technological imperfections: deviation from the nominal coupling length

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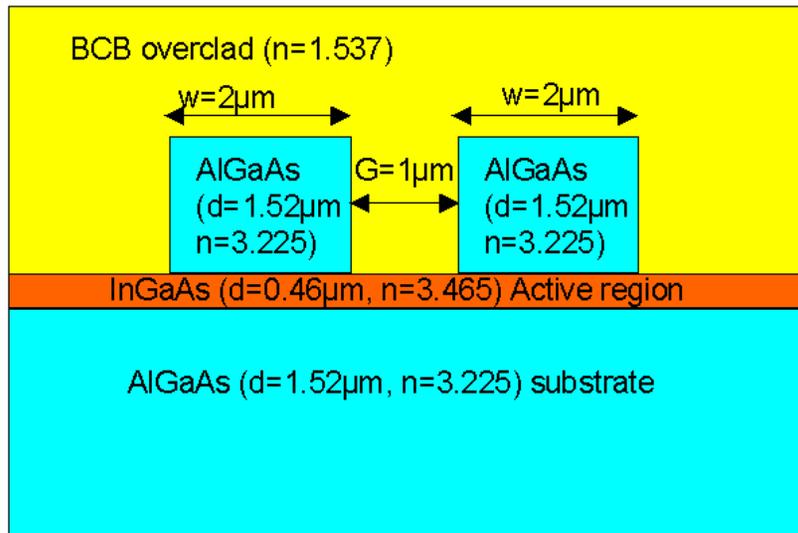


Optimal coupling length $L>2L_c$

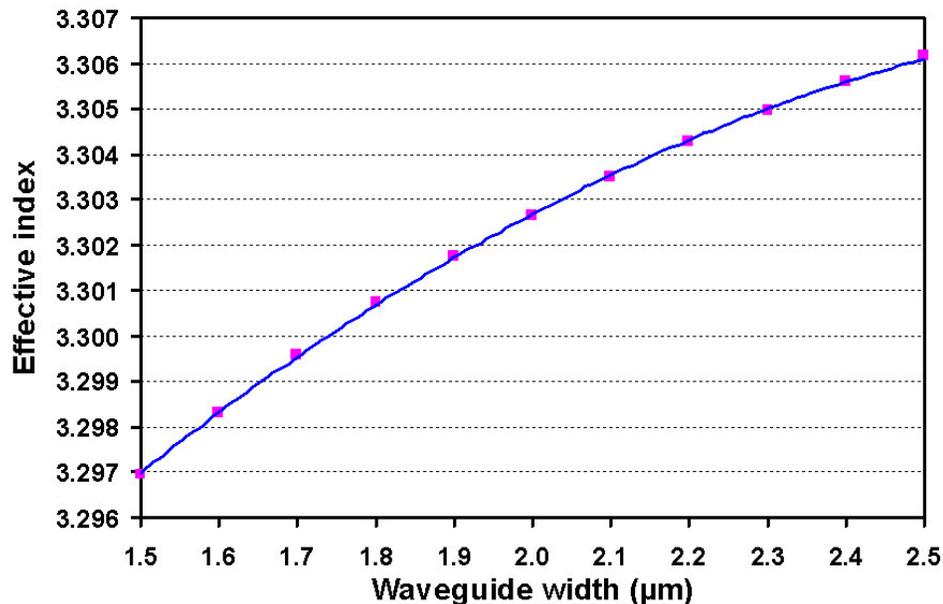


Impact of technological imperfections: mismatch of PT-symmetric coupler effective index

PTSS design

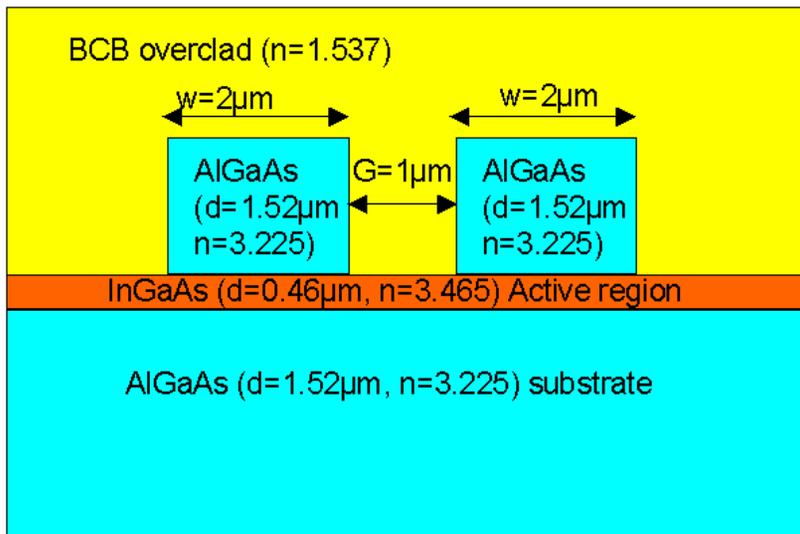


Effective index variation

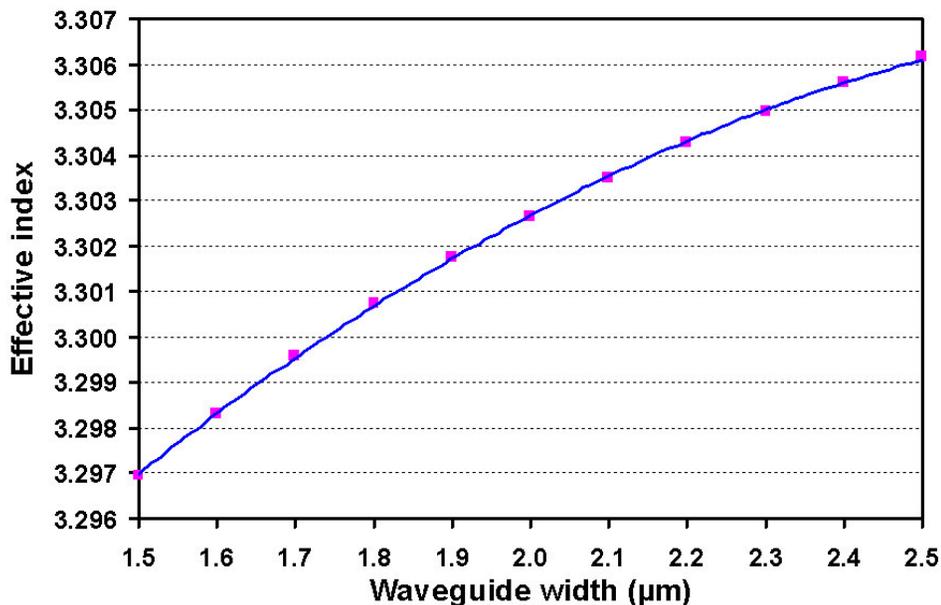


Impact of technological imperfections: mismatch of PT-symmetric coupler effective index

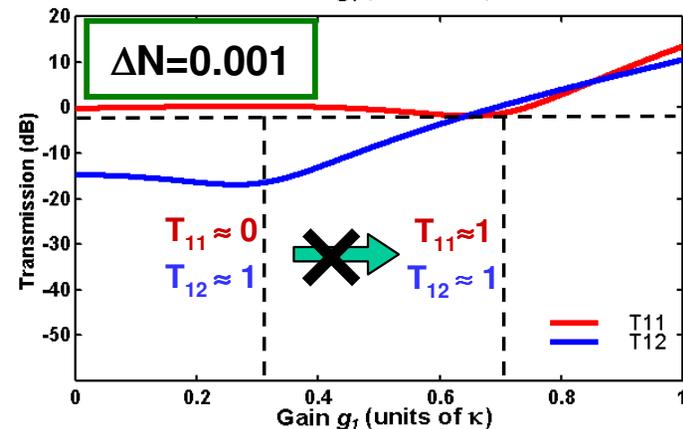
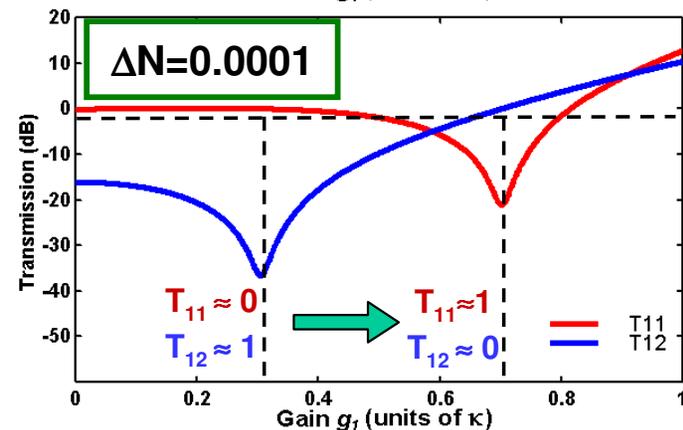
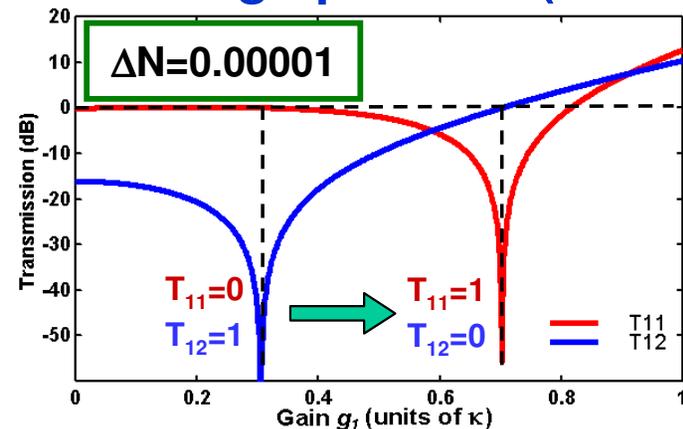
PTSS design



Effective index variation

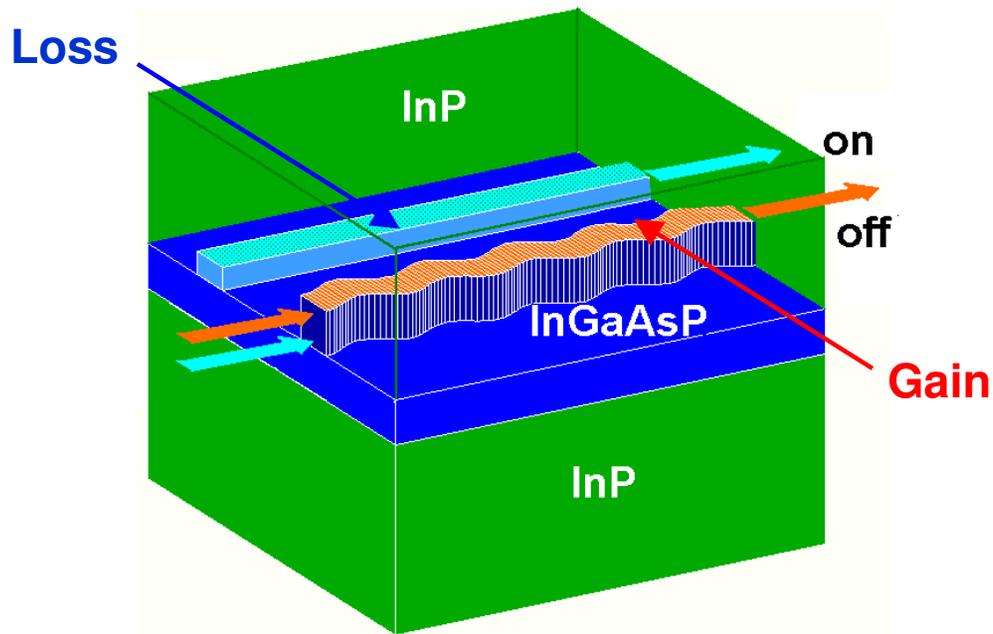


Switching operation ($L=2.1L_c$)



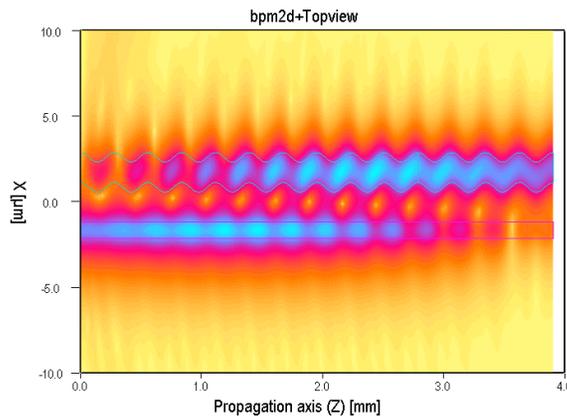
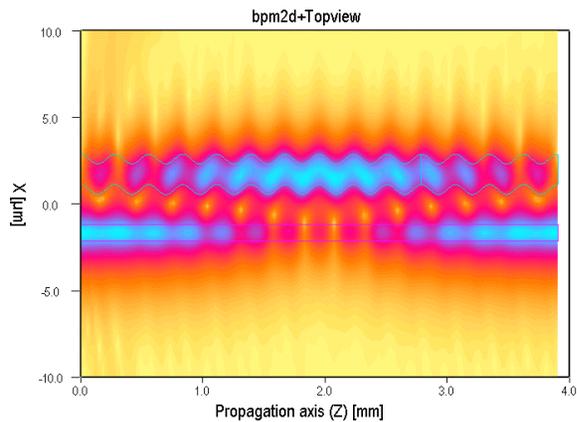
Robust technological design: grating assisted asymmetric PTSS

Grating assisted PTSS



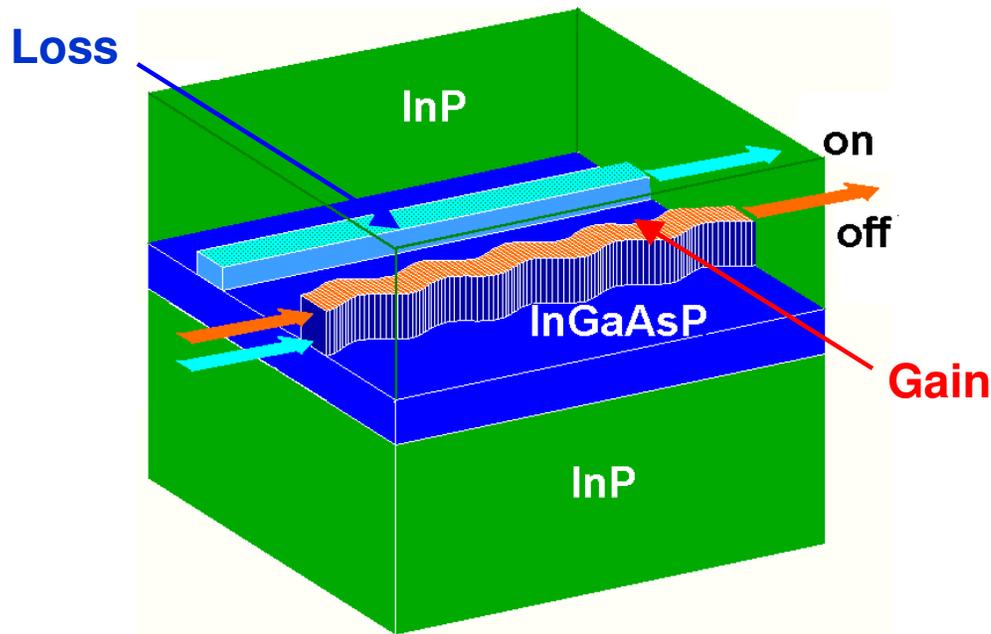
PTSS off

PTSS on



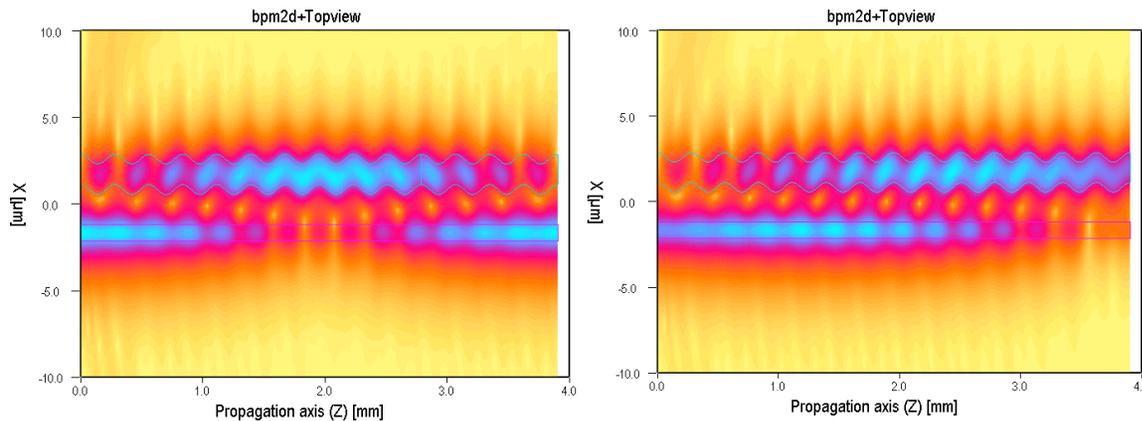
Robust technological design: grating assisted asymmetric PTSS

Grating assisted PTSS

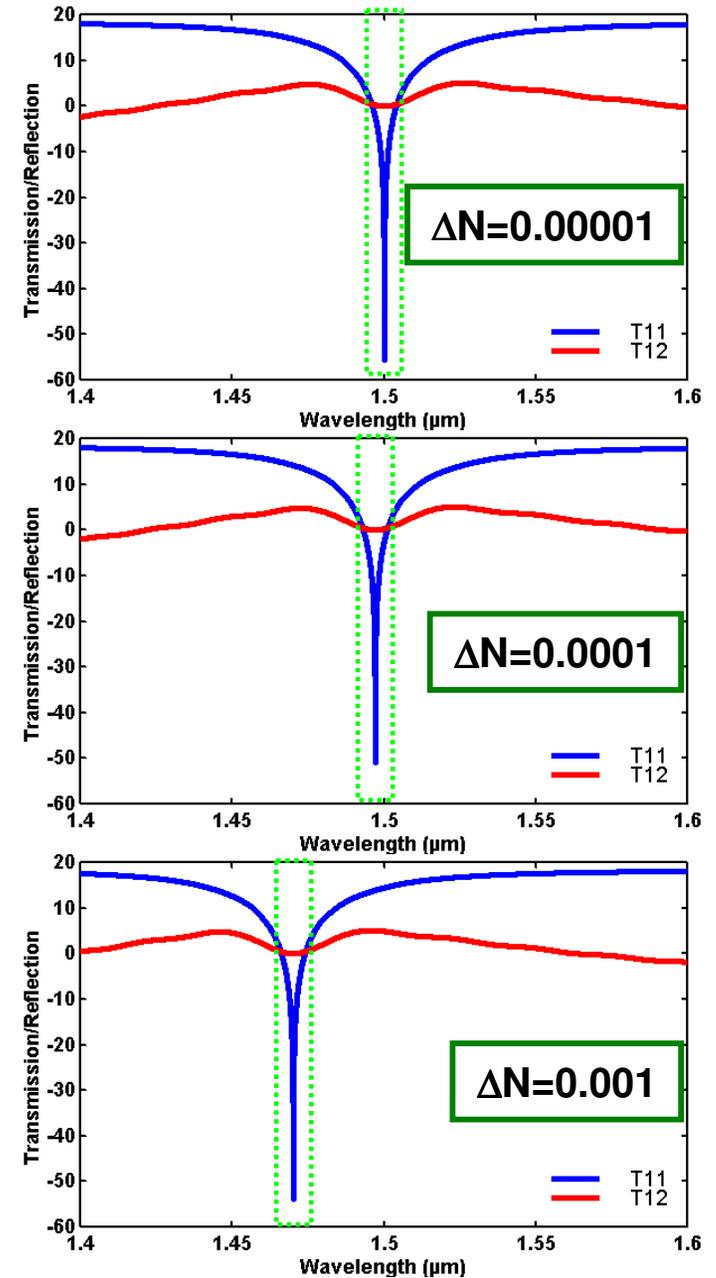


PTSS off

PTSS on



Grating assisted PTSS switching

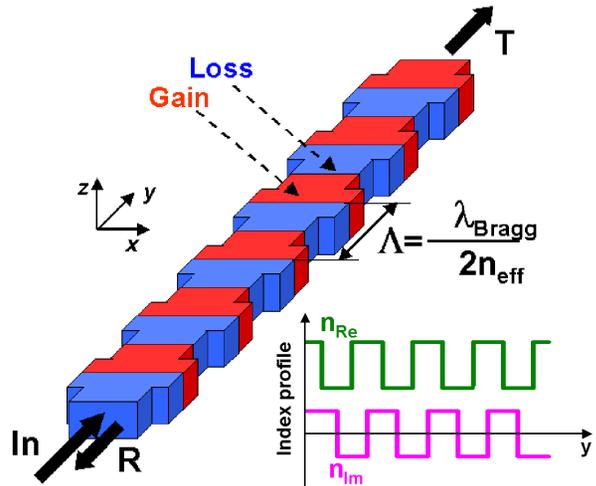


Outline

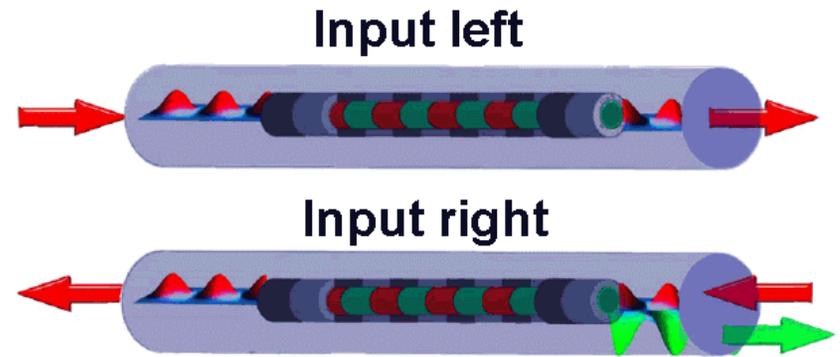
- **Using PT-symmetry for switching applications**
- **Locally PT-symmetric Bragg gratings**
- **PT-symmetry: a new platform for active optical devices**
- **Summary and conclusions**

Non-reciprocal PT-symmetric Bragg type devices

PT-symmetric Bragg grating



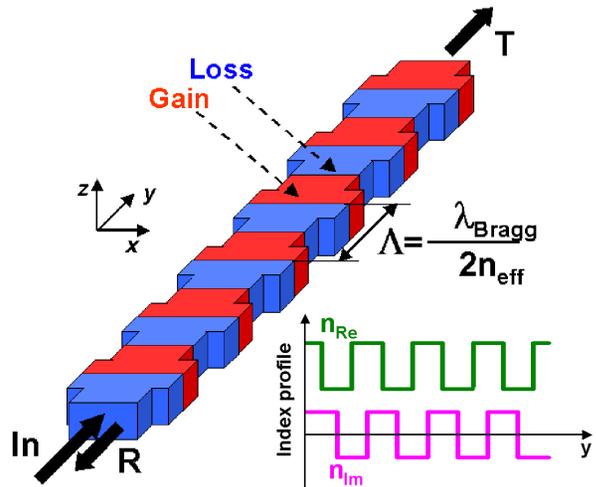
Unidirectional reflectivity



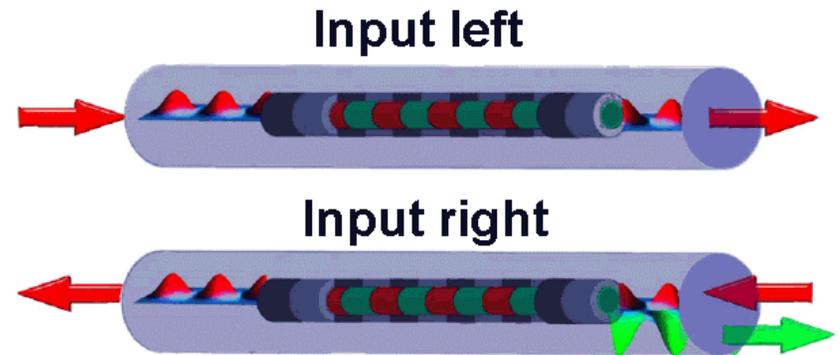
Z. Lin et al, *Phys. Rev. Lett* 106, 213901 (2011)

Non-reciprocal PT-symmetric Bragg type devices

PT-symmetric Bragg grating

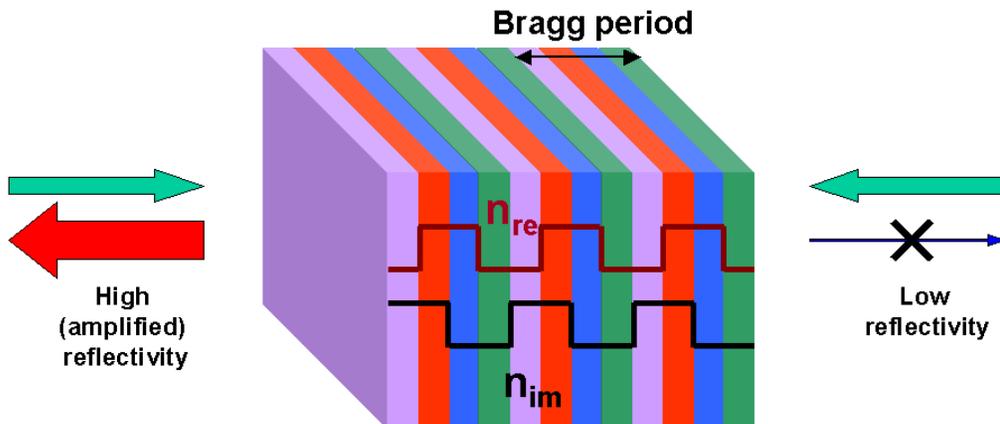


Unidirectional reflectivity



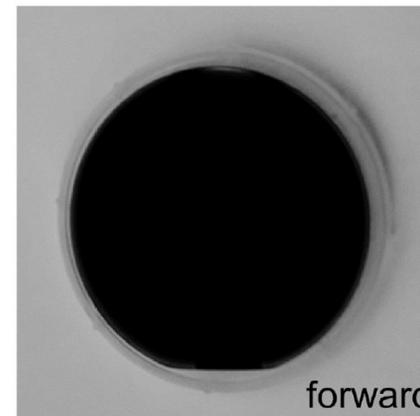
Z. Lin et al, Phys. Rev. Lett 106, 213901 (2011)

PT-symmetric Bragg mirror



Low reflectivity

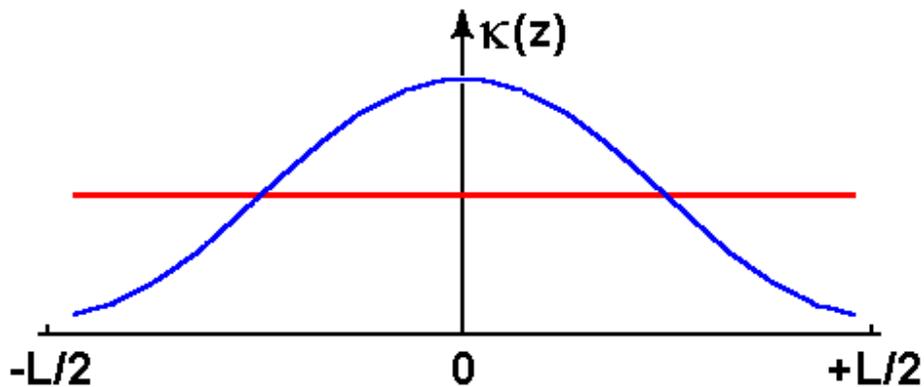
High reflectivity



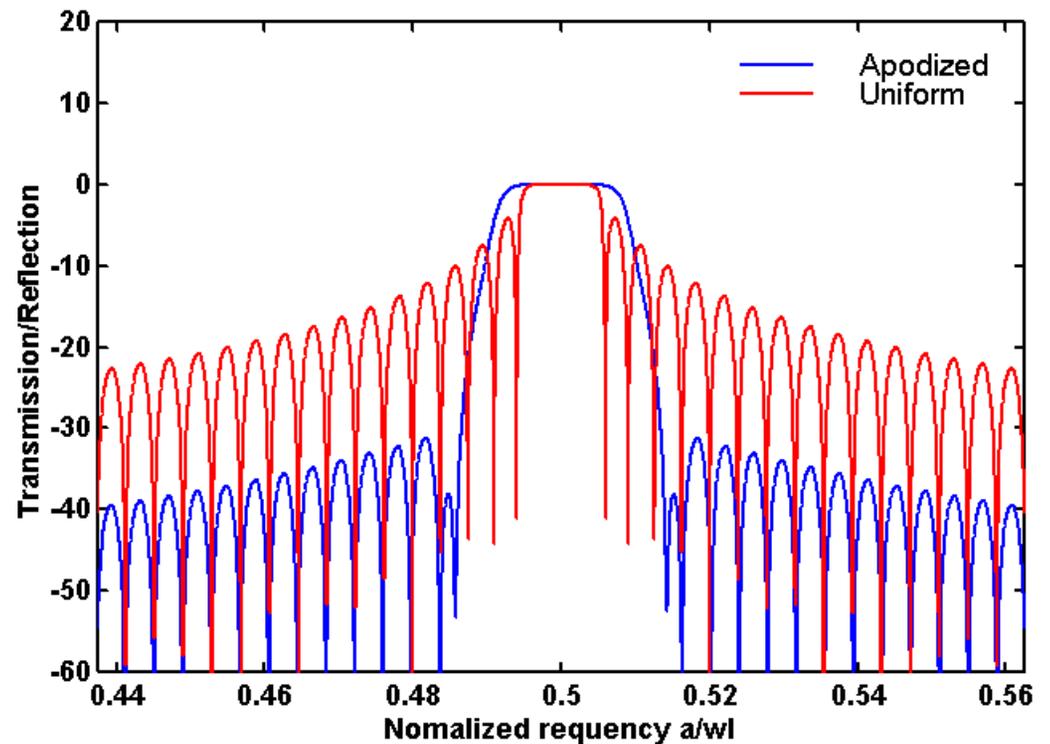
L. Feng et al, Opt. Express 22, 1760–1767 (2014)

Apodization principle: coupling profile tapering

Coupling profile



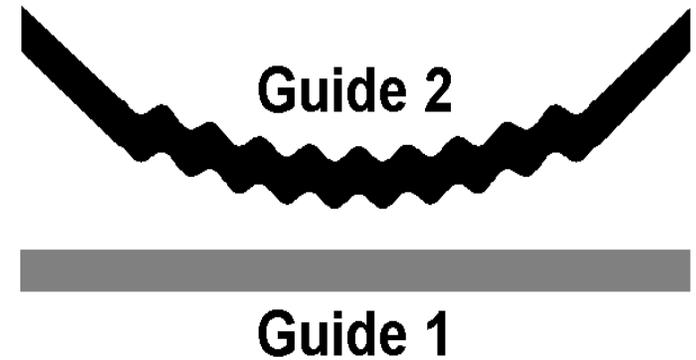
Conventional Bragg grating spectral response



Coupling profile tapering methods

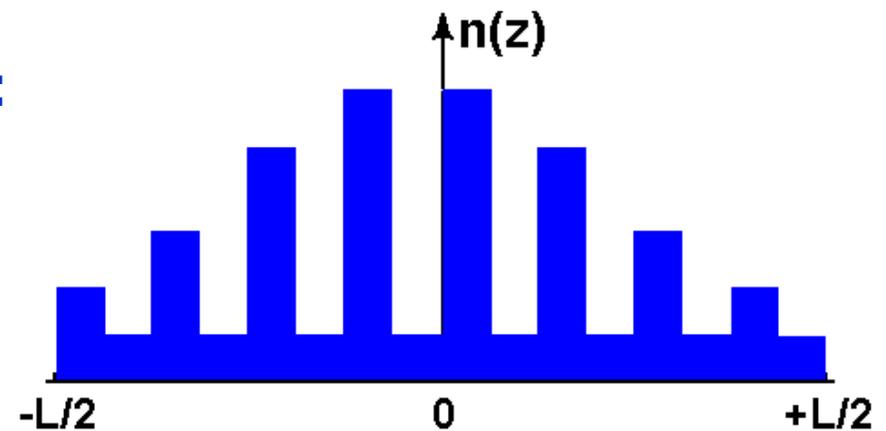
- **Inter-waveguides spacing variation:**

- co- and contra-directional couplers



- **Refractive index contrast modulation:**

- photo-imprinted Bragg gratings
- rugated Bragg mirrors



- **Grating duty ratio variation:**

- co- and contra-directional couplers
- surface corrugated Bragg gratings
- Bragg mirrors



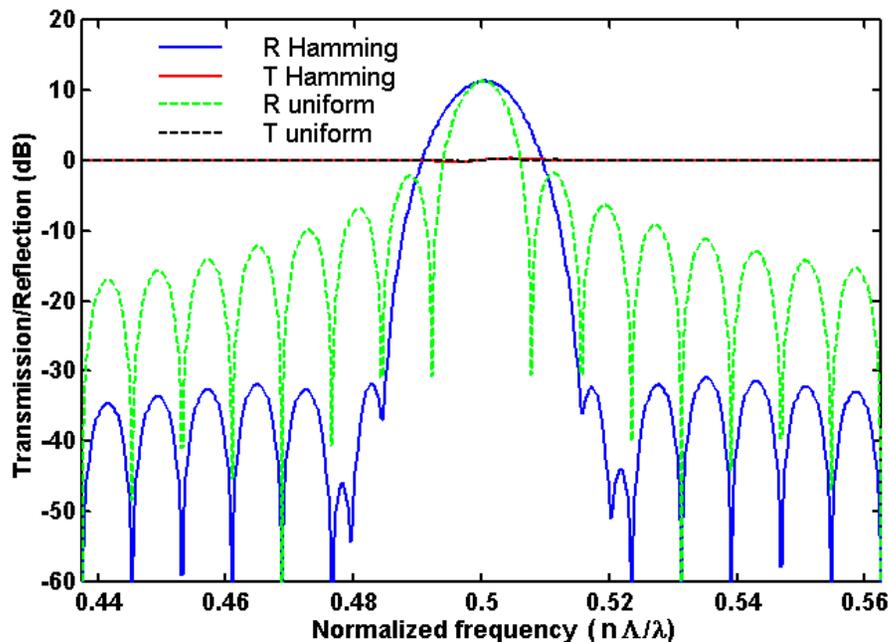
Nonuniform perfectly PT-symmetric Bragg grating

Hamming type apodization of complex index profile

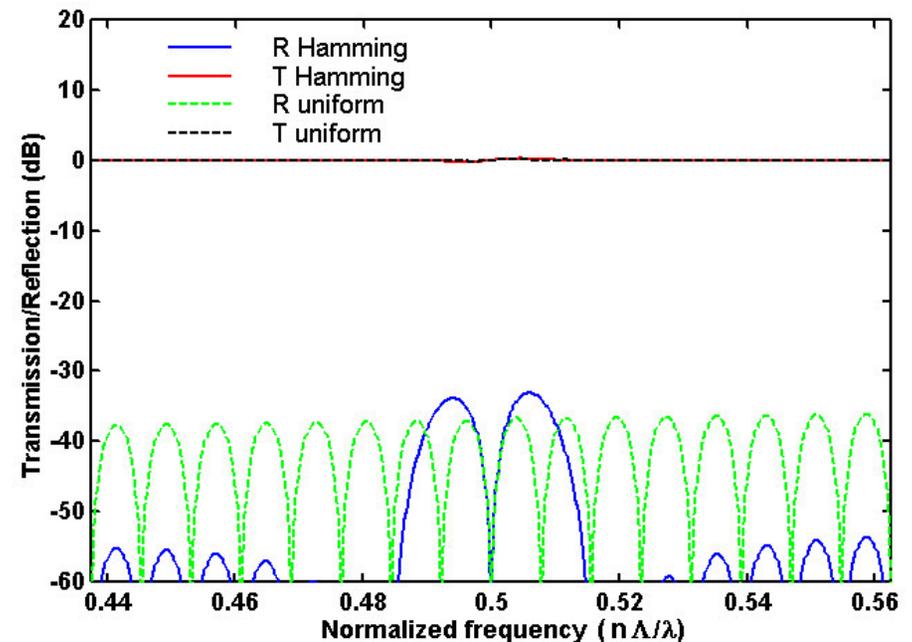
$$n(z) = n_0 + f(z) \Delta n e^{i2\pi z / \Lambda}$$

$$f(z) = 1 + 0.852 \cos(2\pi z / L)$$

Front side incidence (high reflection)



Rear side incidence (low reflection)

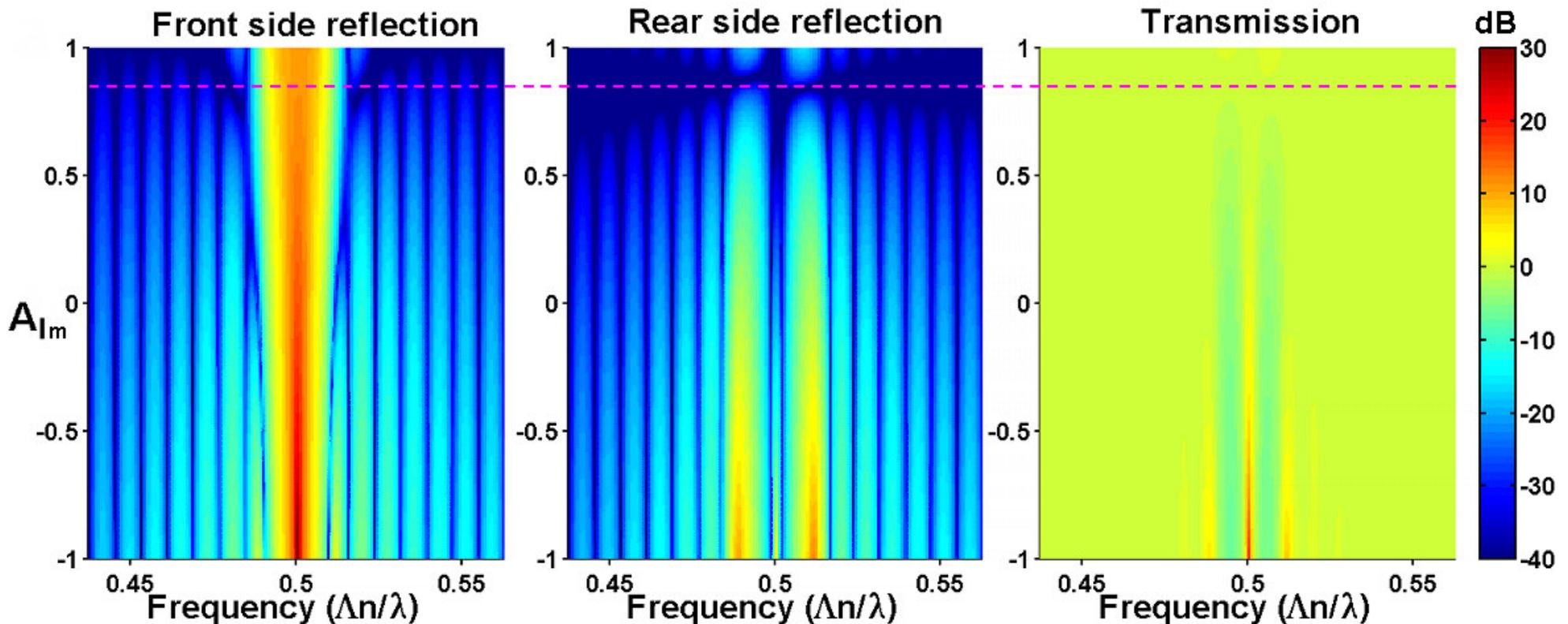


Nonuniform pseudo PT-symmetric Bragg grating

Pseudo PT-symmetric apodization of complex index profile

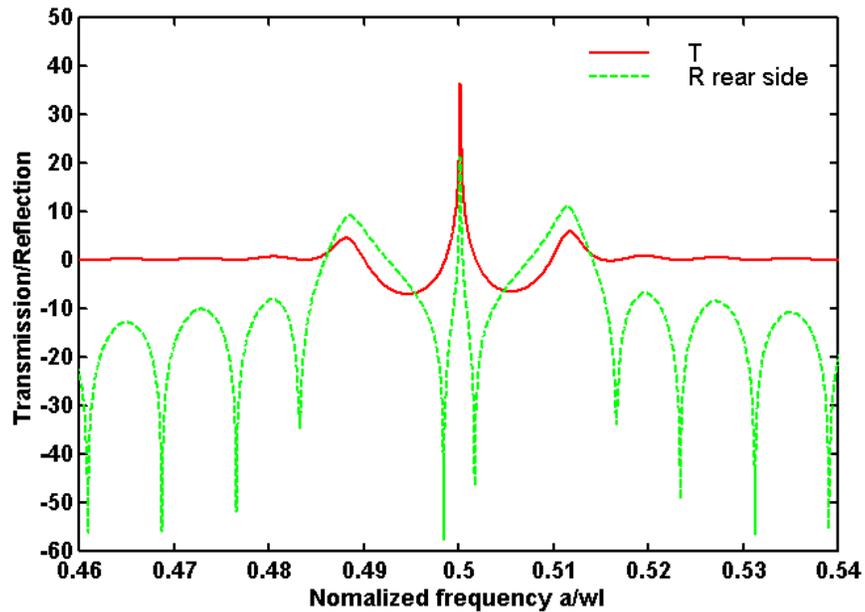
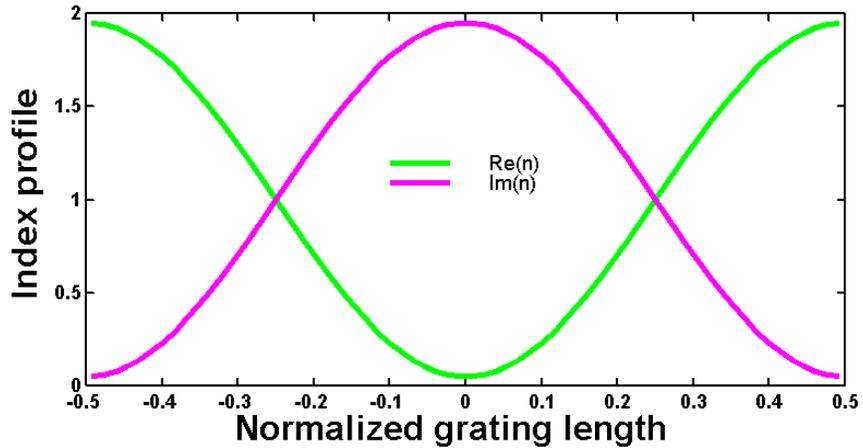
$$n(z) = n_0 + f(z) \left(A_{\text{Re}} \cos(2\pi z / L) + iA_{\text{Im}} \sin(2\pi z / L) \right)$$

Spectral maps ($A_{\text{re}}=0.852$)



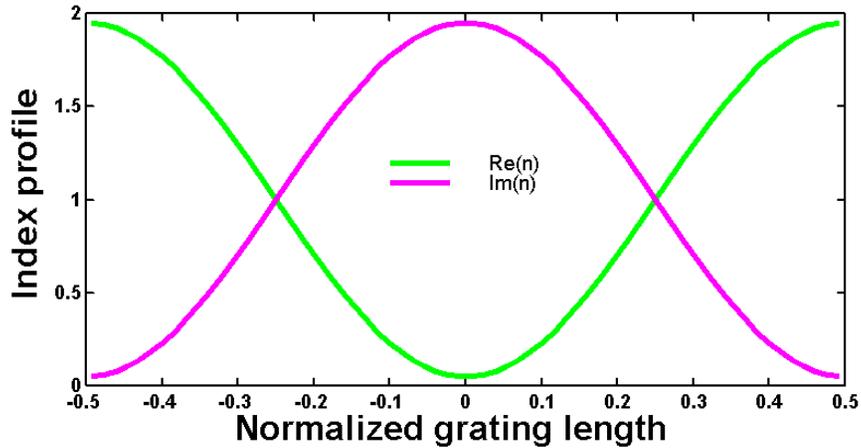
Additional functionalities of locally PT-symmetric Bragg gratings

Single mode amplifier
($A_{\text{Re}}=-0.95$; $A_{\text{Im}}=0.95$)

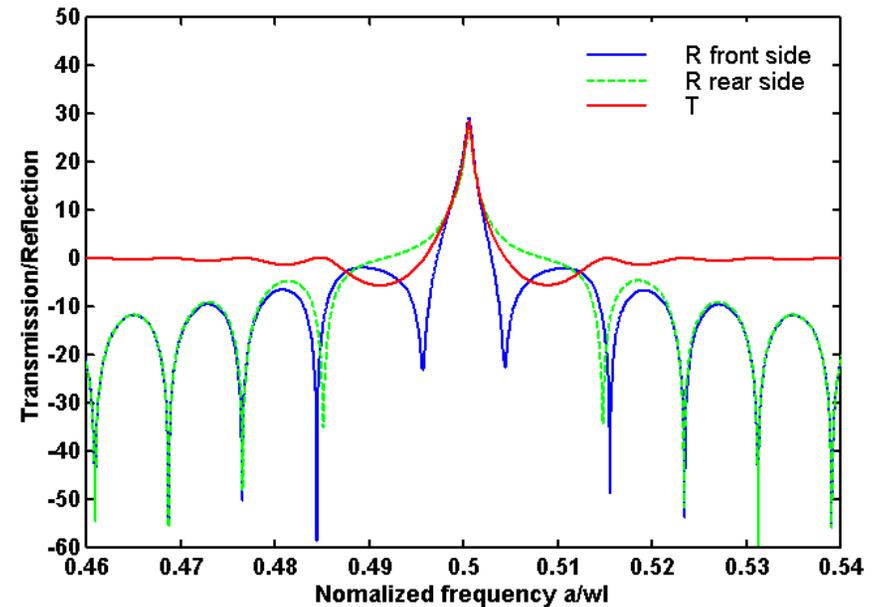
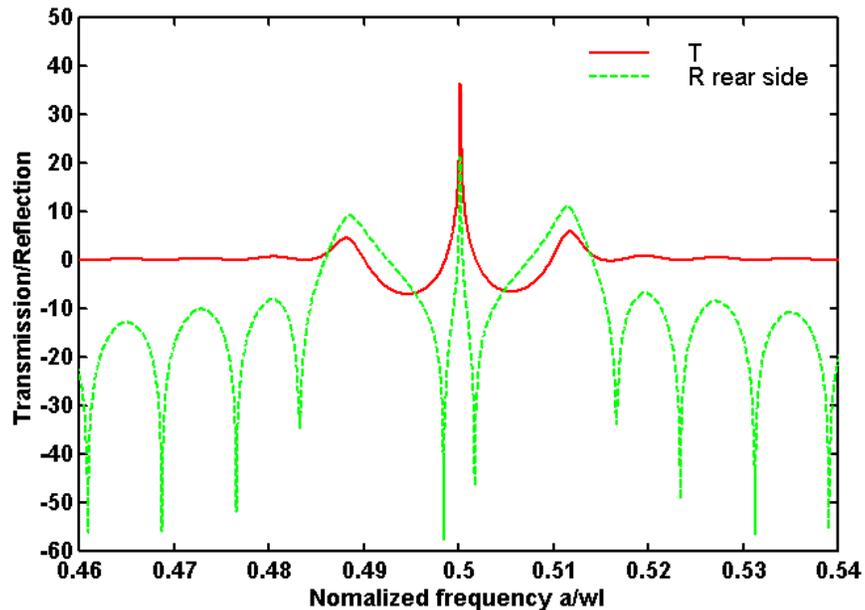
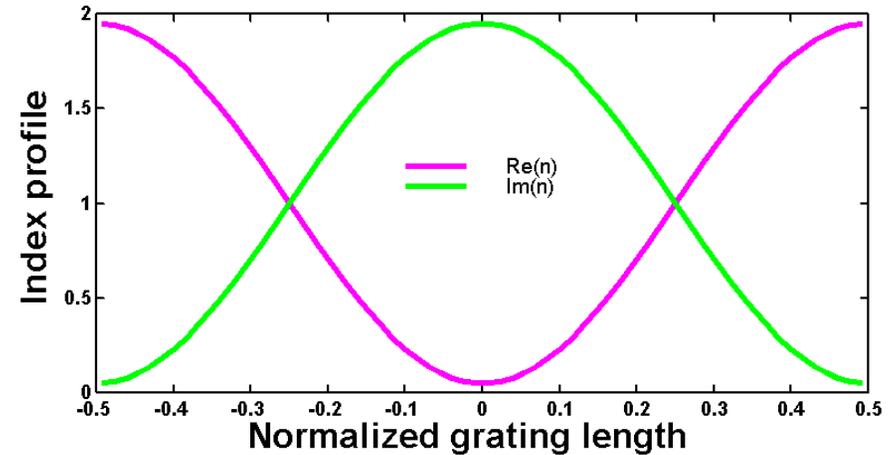


Additional functionalities of locally PT-symmetric Bragg gratings

Single mode amplifier
($A_{Re}=-0.95$; $A_{Im}=0.95$)

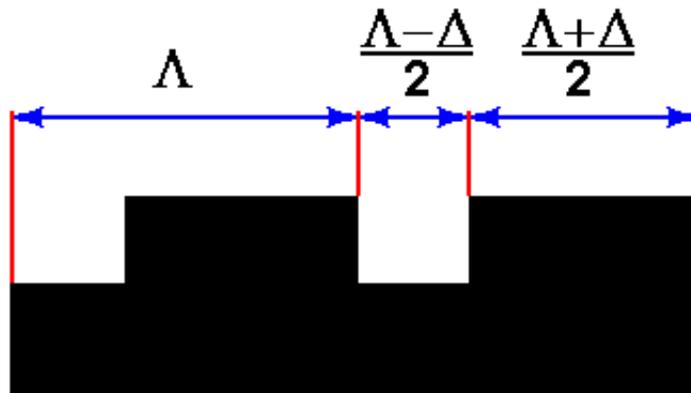


Single mode DFB laser
($A_{Re}=0.95$; $A_{Im}=-0.95$)



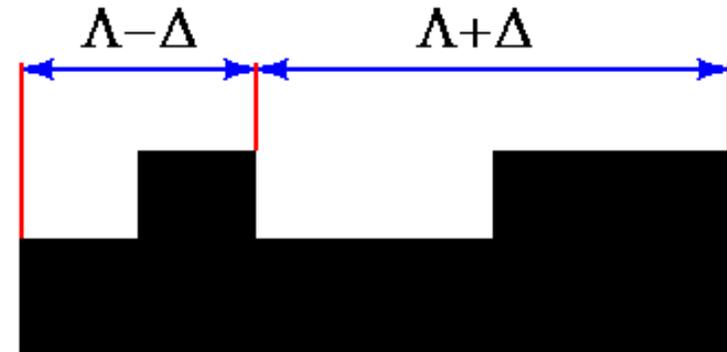
Grating duty cycle modulation methods

Basic Duty Cycle



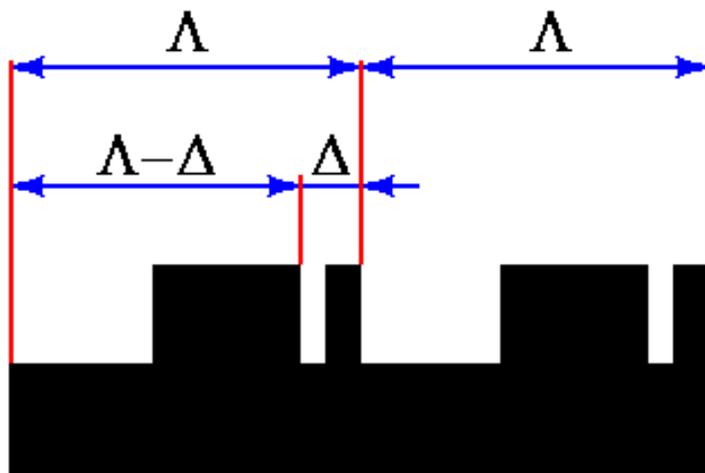
H. Sakata, Opt. Lett., 17, (1992)

Off-Resonance



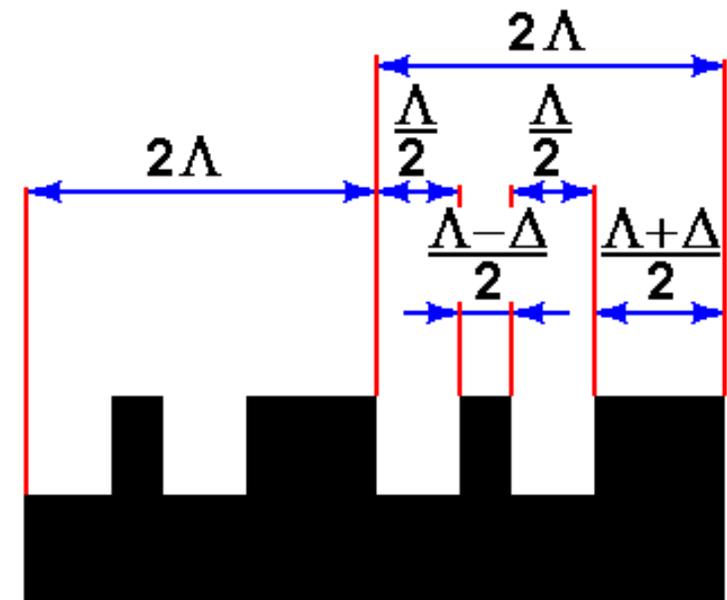
A. Lupu, et al., OFC/IOOC (1999)

Phase Shifted Pair Gratings



D.-B. Kim et al., Photon. Technol. Lett, 10, (1998)

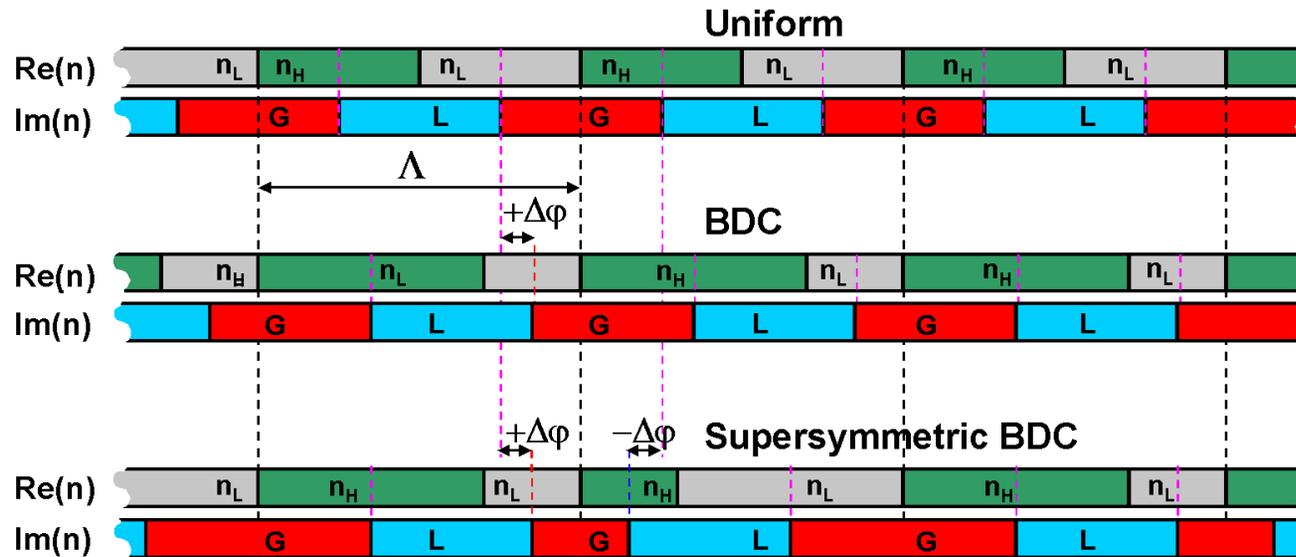
Concatenated Gratings



D. Wiesmann et al., Photon. Technol. Lett., 12, (2000)

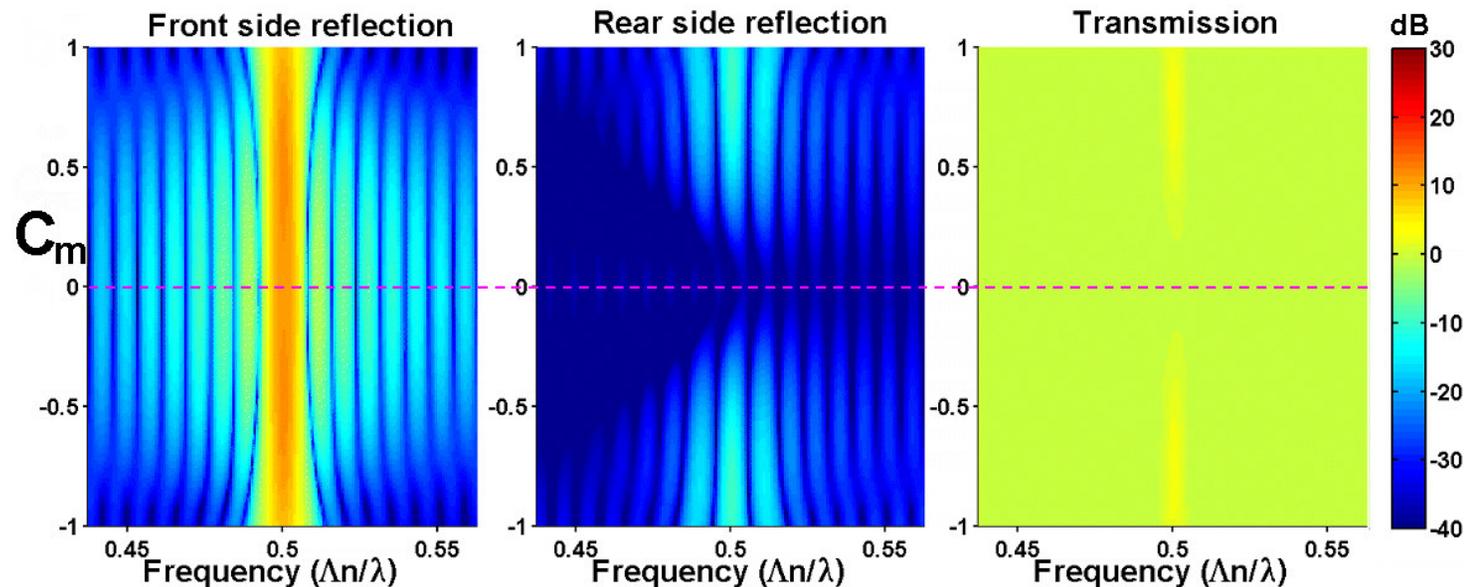
Duty cycle modulated binary PT-symmetric gratings

Duty cycle modulation schemes



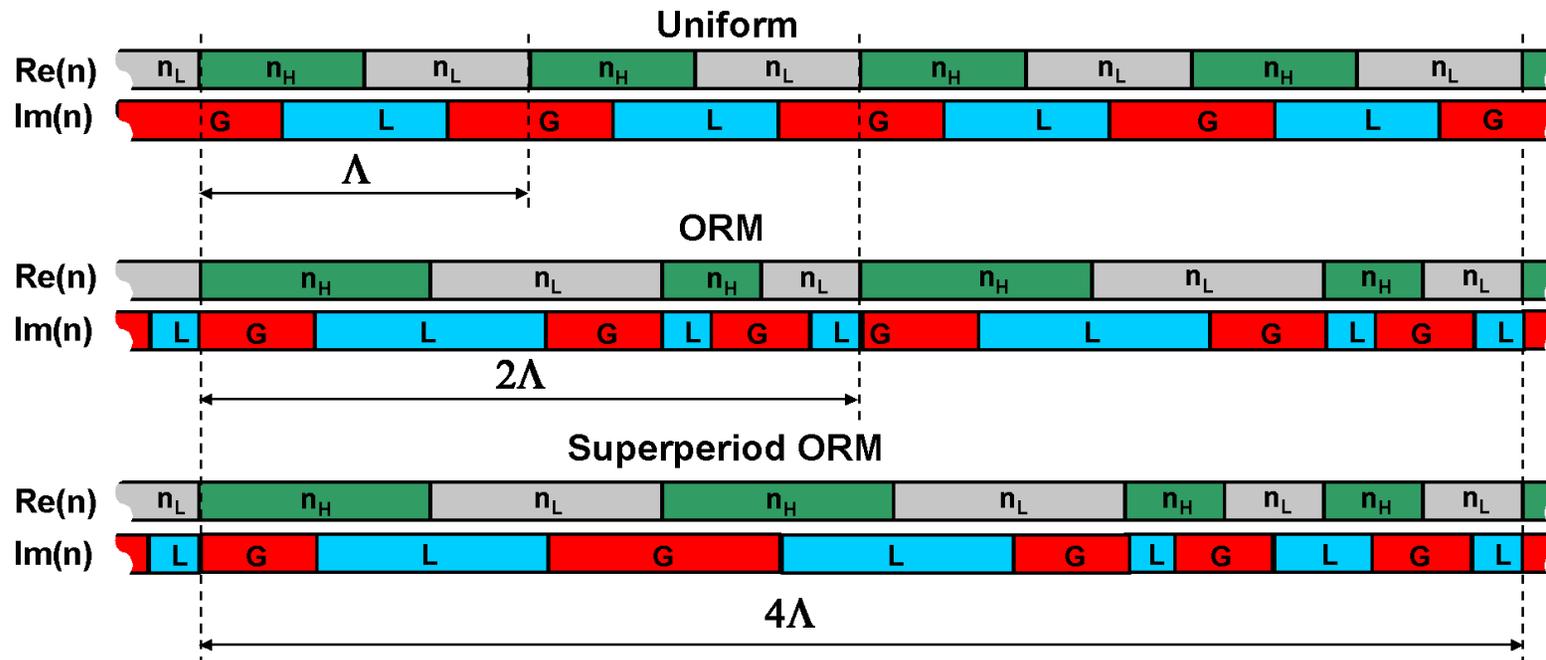
A. Lupu, H. Benisty, A. Lavrinenko, JTSQE 2016

Spectral maps (supersymmetric BDC)



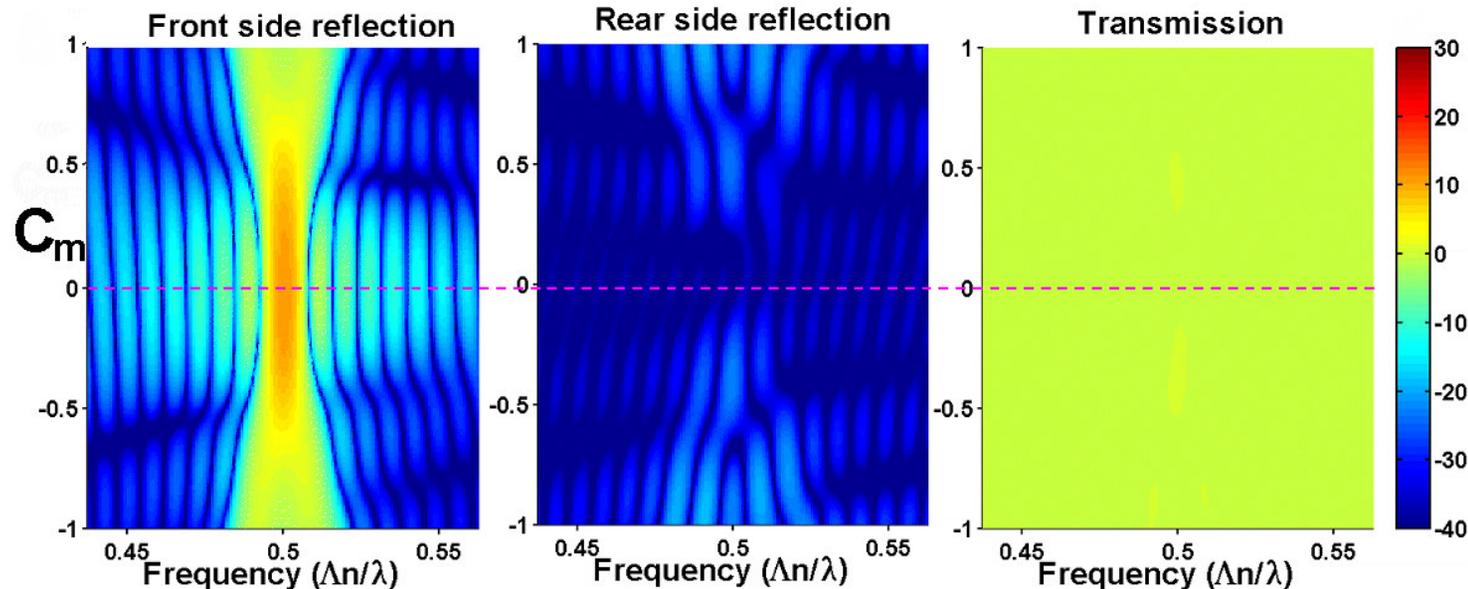
Period modulated binary PT-symmetric gratings

Grating period modulation schemes



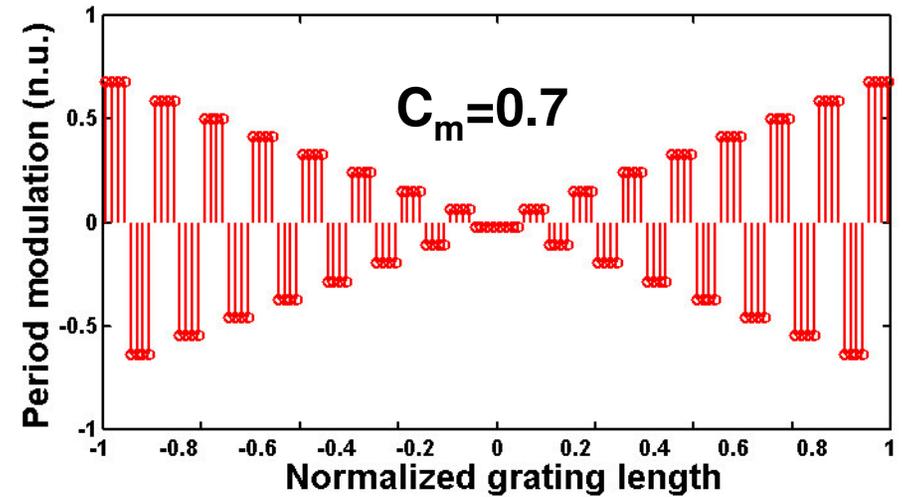
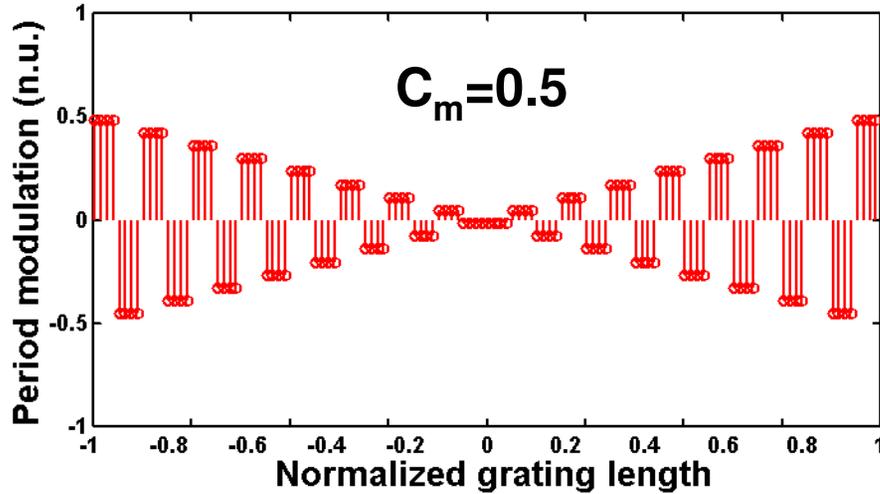
A. Lupu, H. Benisty, A. Lavrinenko, JTSQE 2016

Spectral maps (superperiod ORM)

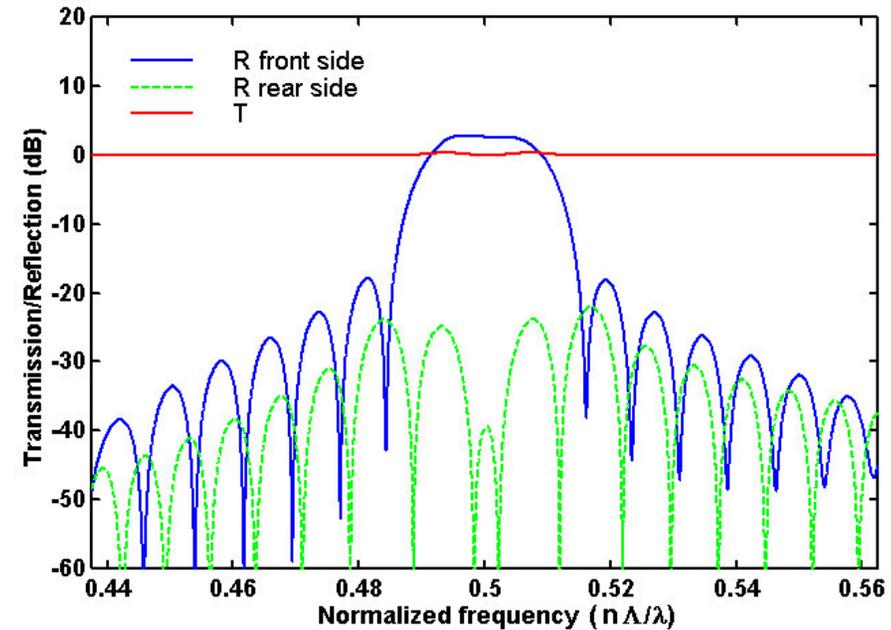
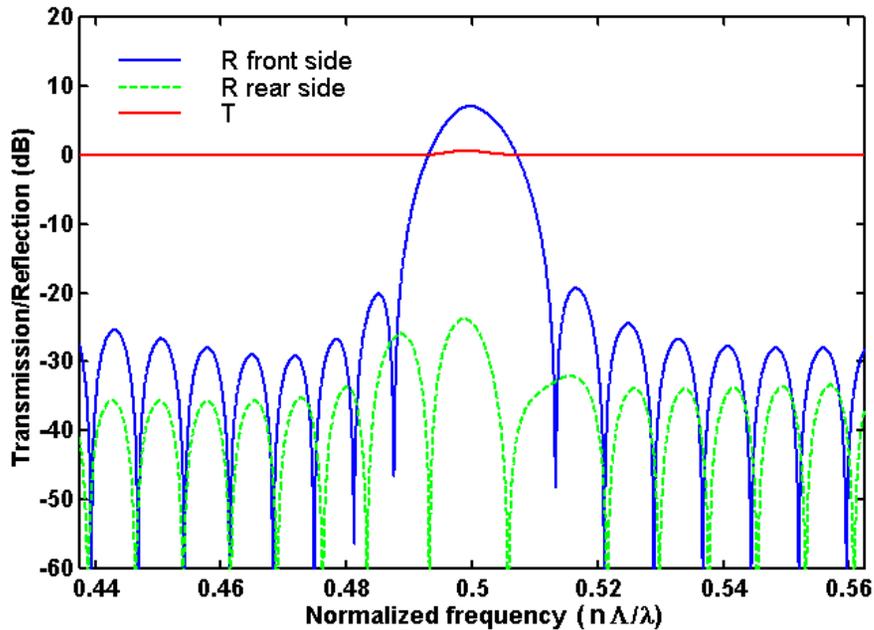


Tailoring spectral properties of locally Parity-Time symmetric Bragg gratings

Grating period modulation



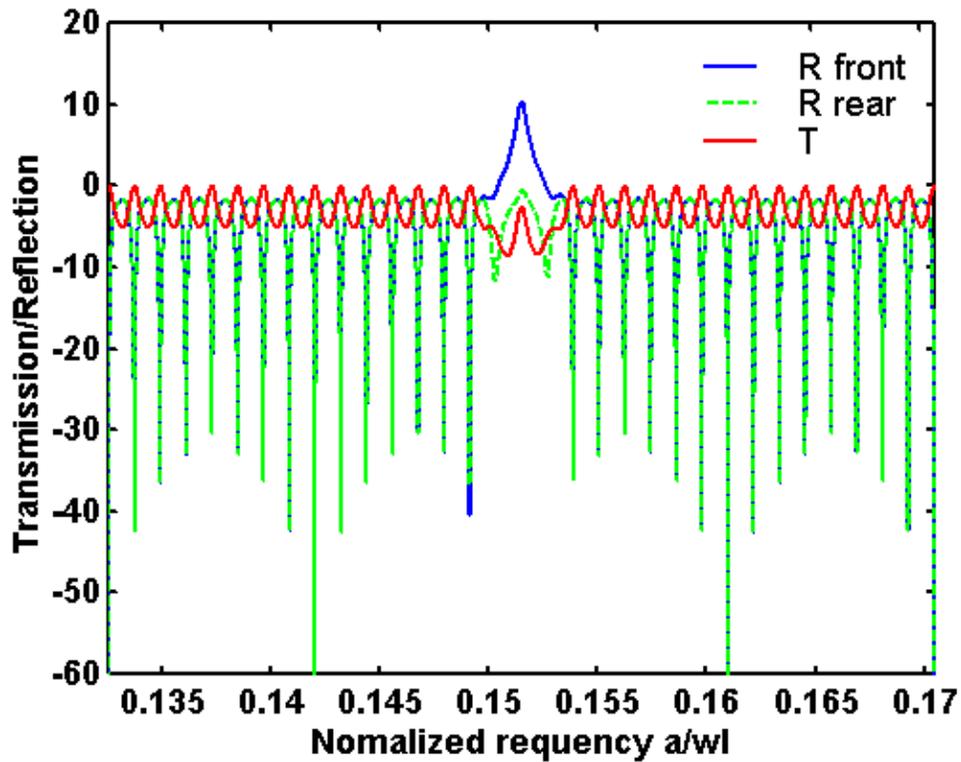
Spectral response



Impact of PT-symmetric grating impedance mismatch with external media

Hamming type apodization of complex index profile

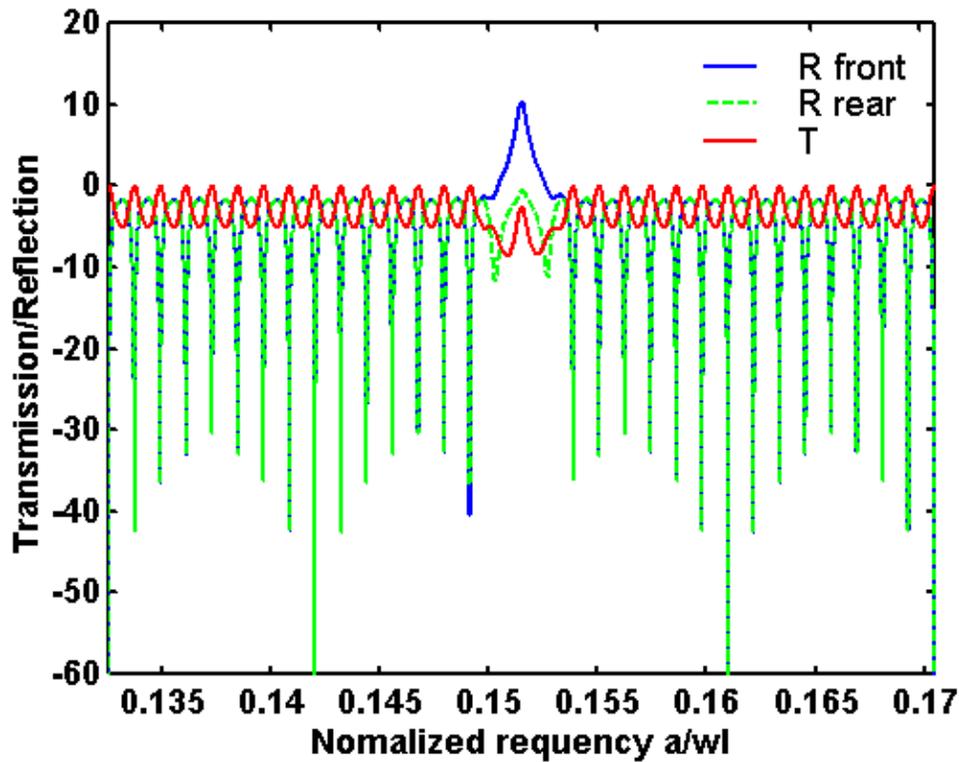
No antireflection coating



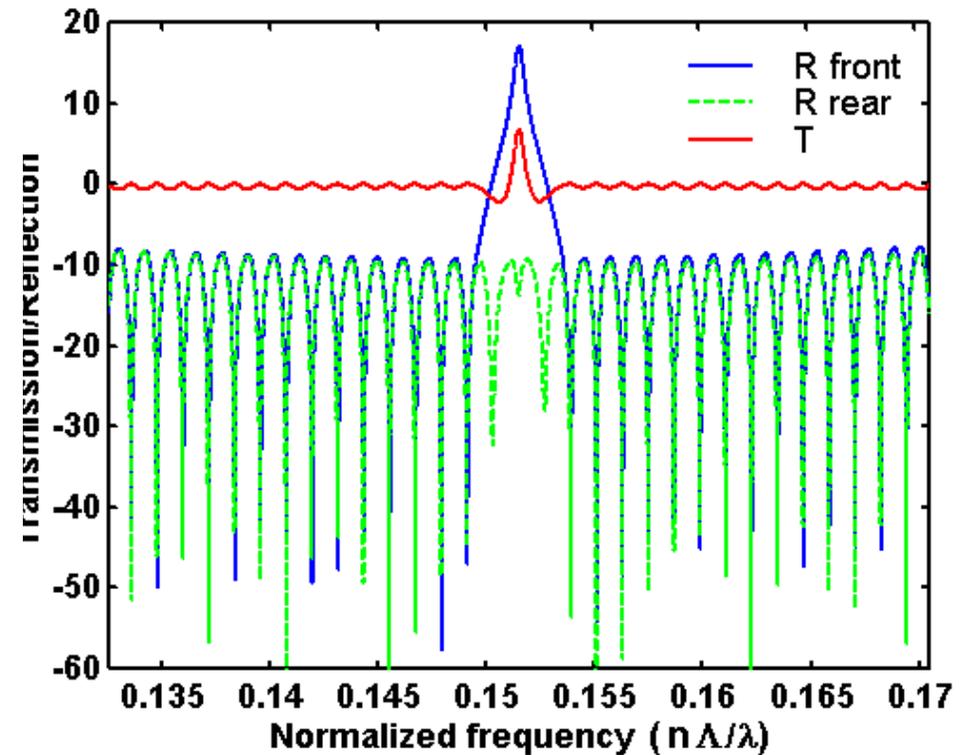
Impact of PT-symmetric grating impedance mismatch with external media

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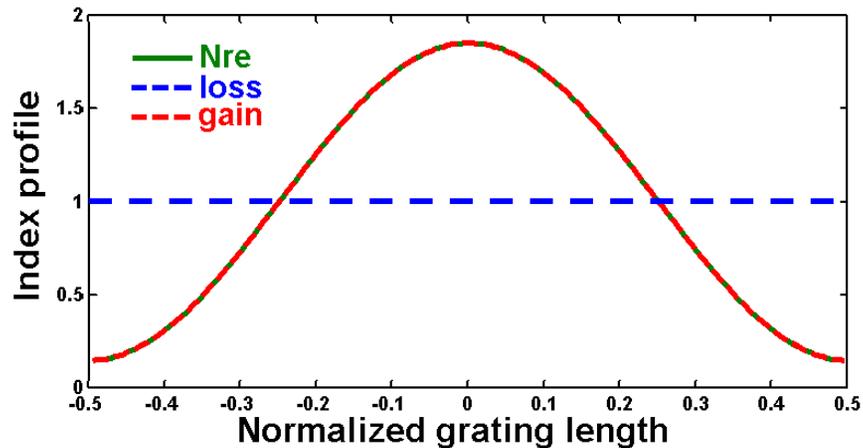
Antireflection coating



Toward active tailoring of the spectral response

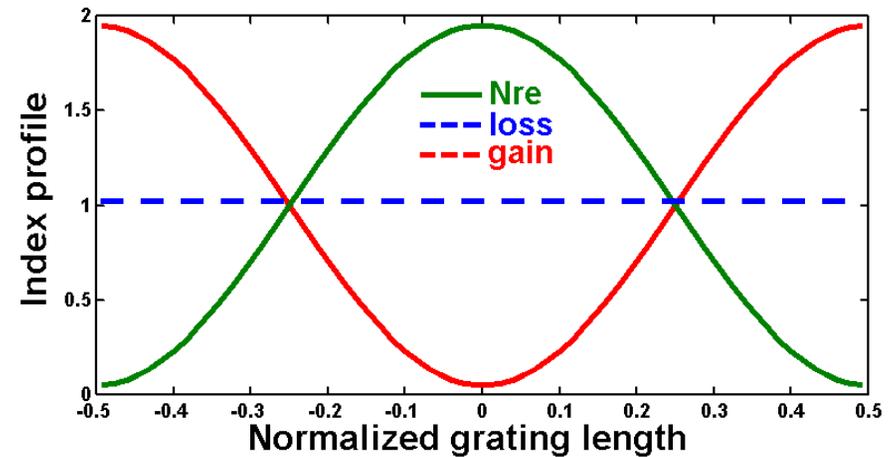
Complex index modulation

$$A_{\text{Re}} = -0.85; A_{\text{loss}} = 0; A_{\text{gain}} = 0.85$$



Complex index modulation

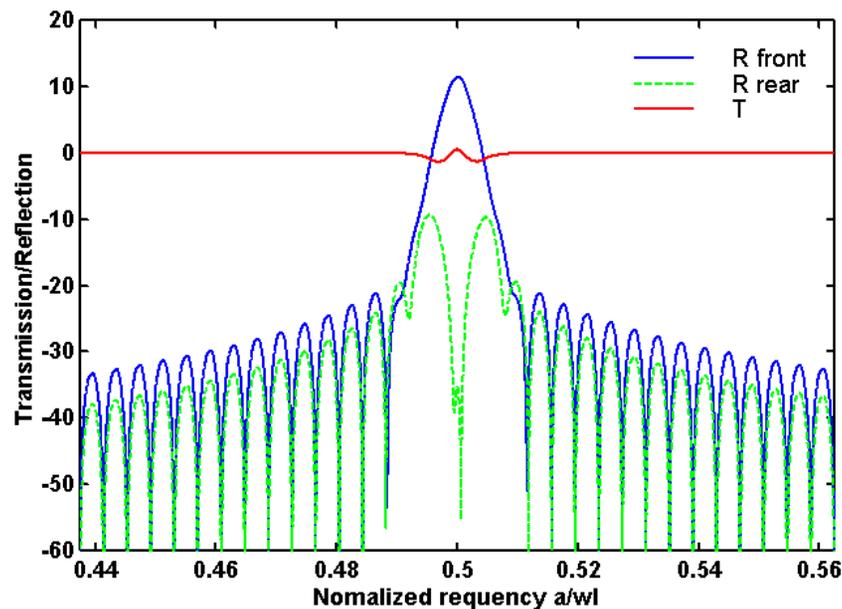
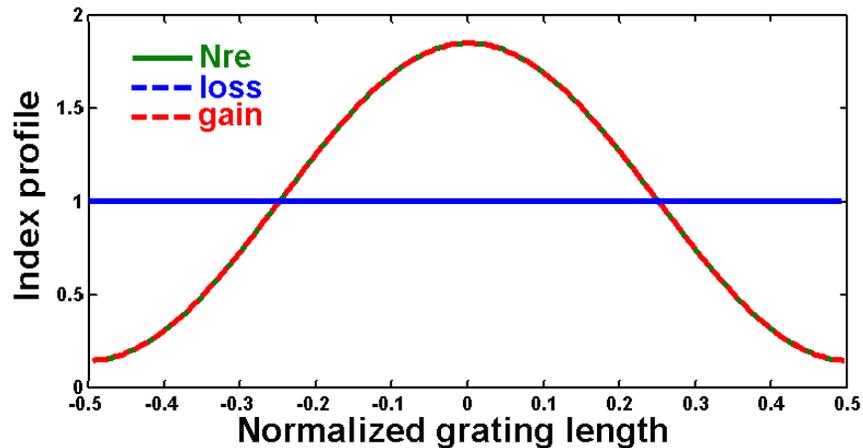
$$A_{\text{Re}} = -0.85; A_{\text{loss}} = 0; A_{\text{gain}} = -0.85$$



Toward active tailoring of the spectral response

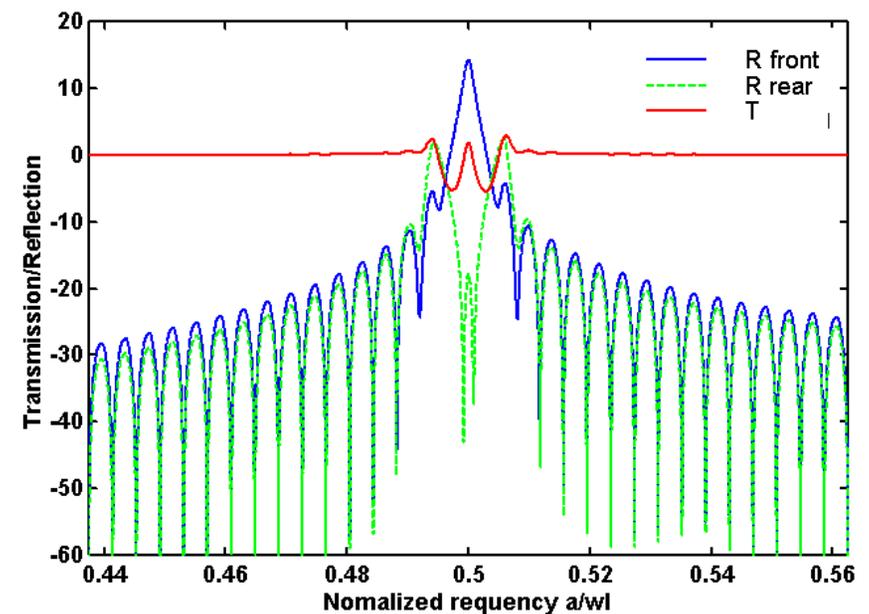
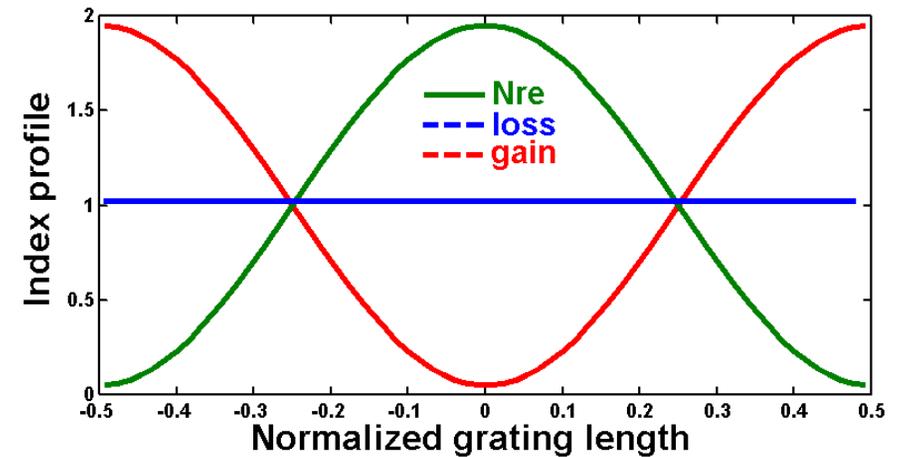
Complex index modulation

$$A_{\text{Re}} = -0.85; A_{\text{loss}} = 0; A_{\text{gain}} = 0.85$$



Complex index modulation

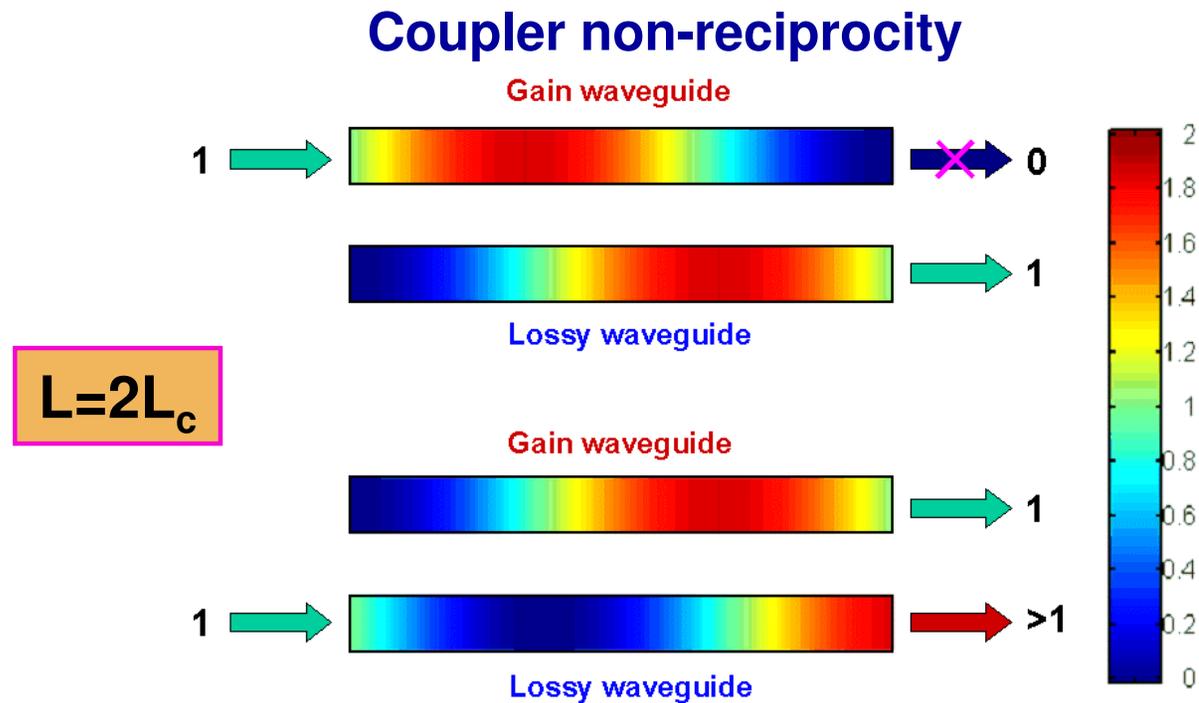
$$A_{\text{Re}} = -0.85; A_{\text{loss}} = 0; A_{\text{gain}} = -0.85$$



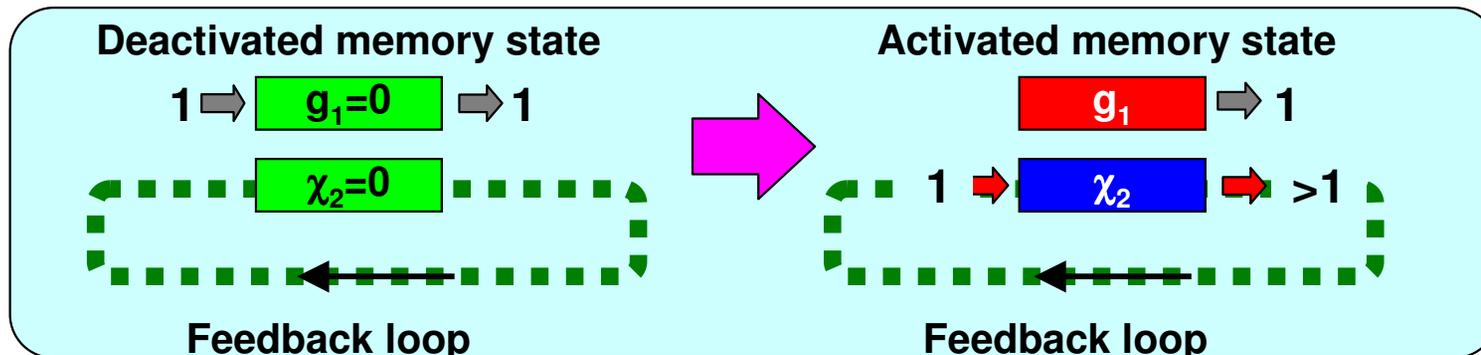
Outline

- **Using PT-symmetry for switching applications**
- **Locally PT-symmetric Bragg gratings**
- **PT-symmetry: a new platform for active optical devices**
- **Summary and conclusions**

PT-symmetric spatial non-reciprocity: toward buffer memory applications



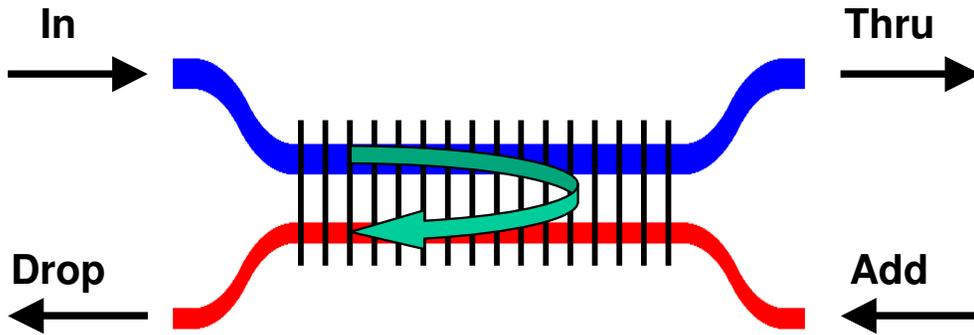
Buffer memory application



See also: M. Kulishov, et al, "Trapping light in a ring resonator using a grating assisted coupler with asymmetric transmission," Opt. Express 13, 3567 (2005)

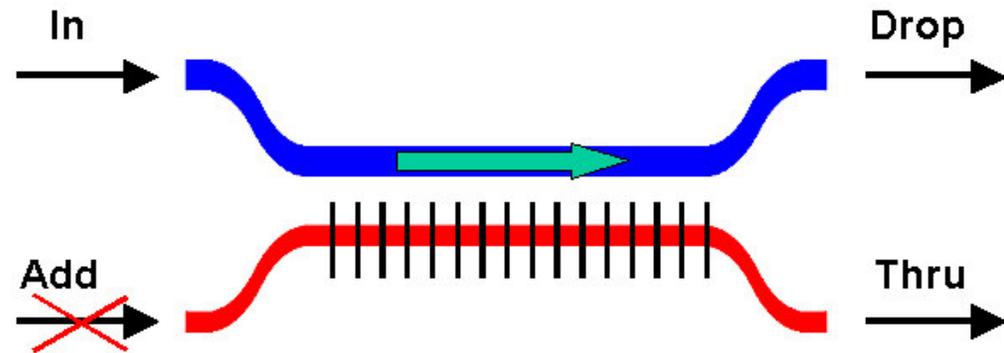
4 ports Bragg grating optical add-drop demultiplexers overview

Contra-directional



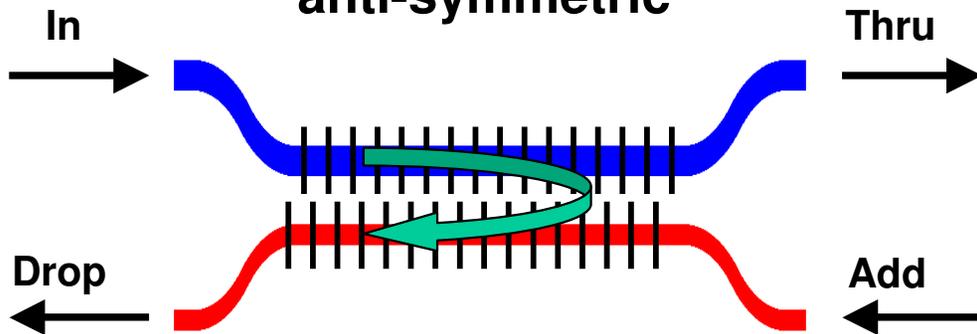
C. Elachi, C. Yeh, Opt. Comm. 7, 201 (1973)

Frustrated coupling



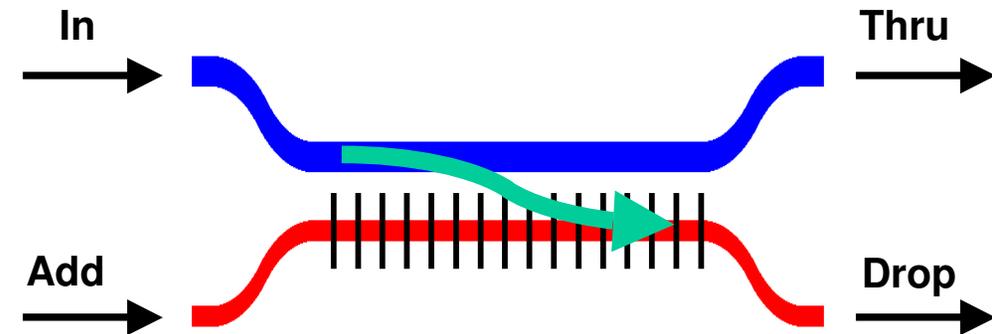
J.-L. Archambault et al, Opt. Lett. 19,180 (1994)

Contra-directional anti-symmetric



Perrone et al, J. Lightwave Technol. 19, 1943 (2001)

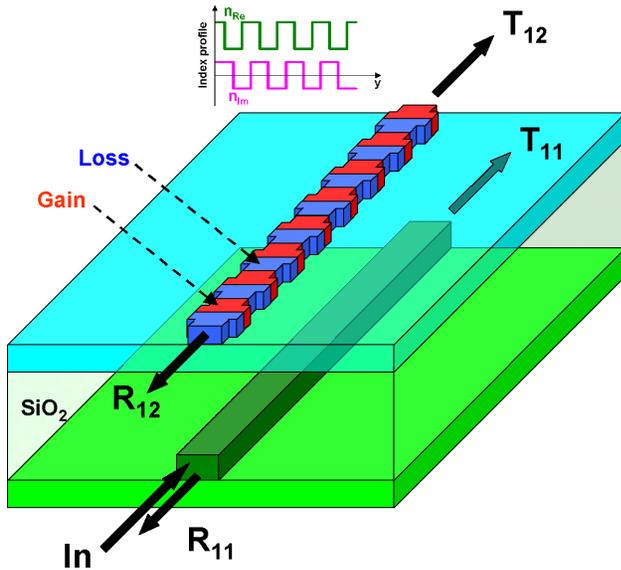
Co-directional



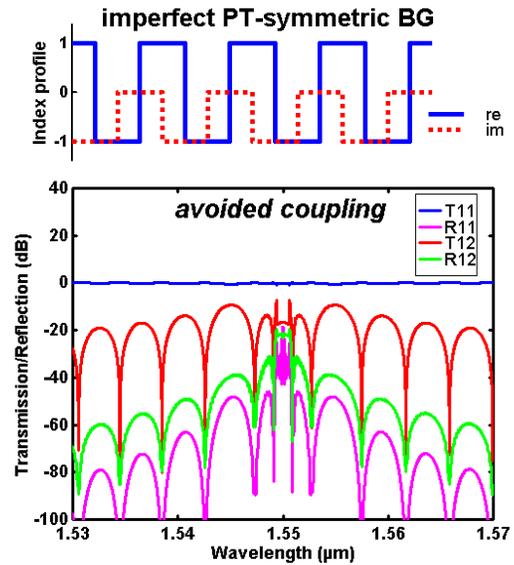
A. Ankiewicz et al, 31, 2151 (1997)
K. Muhieddine et al, Opt. Express 18, 23183 (2010)
A. Lupu et al, Opt. Express 19, 1246 (2011)

PT-symmetric tunable add-drop

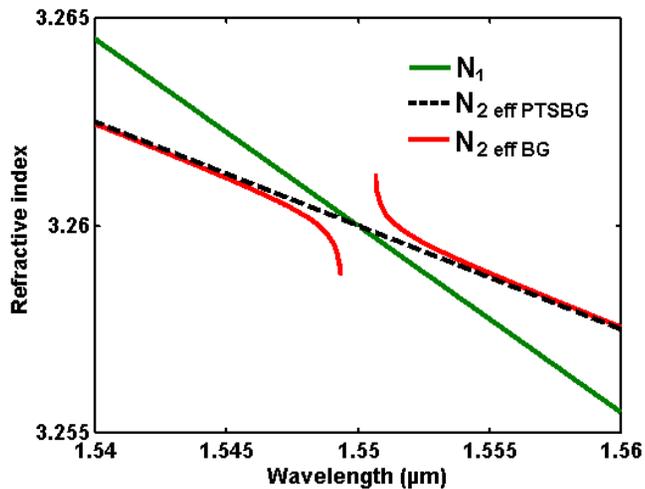
Vertical PTSBG directional coupler



Gain off state

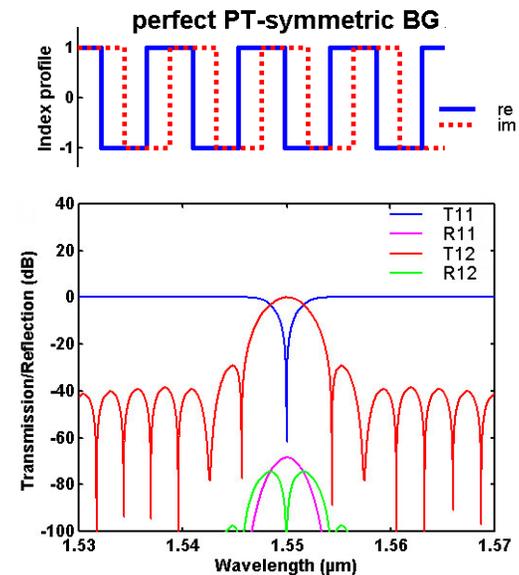


Switch operation principle



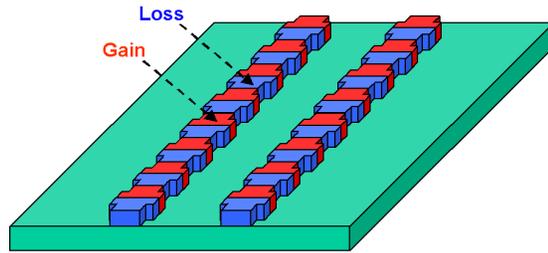
A. Lupu, H. Benisty, et al., PNFA 2014

Gain on state

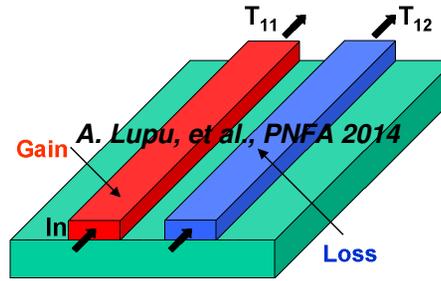


PT-symmetric functional devices

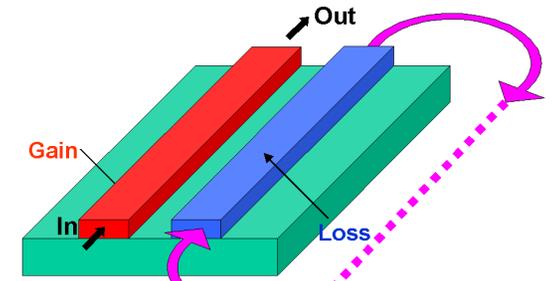
Coherent perfect absorber



PT-symmetric switch



Buffer memory

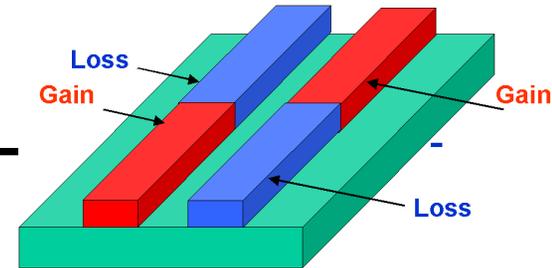
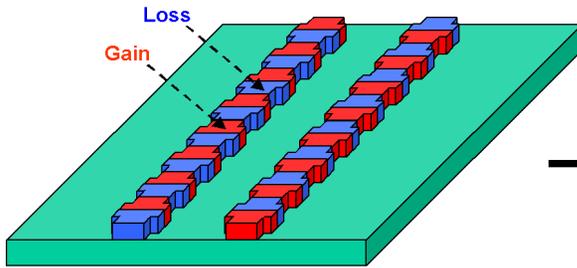


A. Lupu, H. Benisty. et al, Opt. Exp. 2013

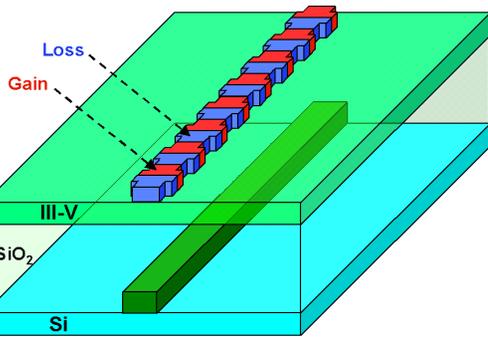
H. Benisty... A. Lupu, et al., Opt. Exp. 2011

A new platform for active optical devices

Single mode amplifier

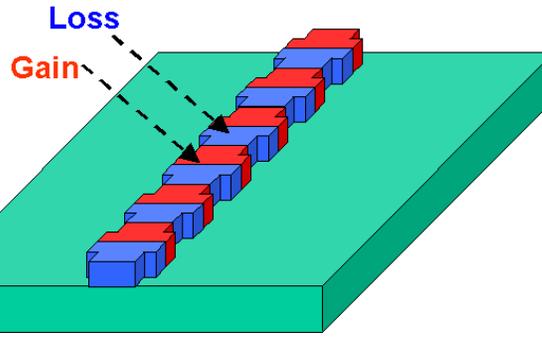


Binary phase modulator ($0 \rightarrow \pi$)

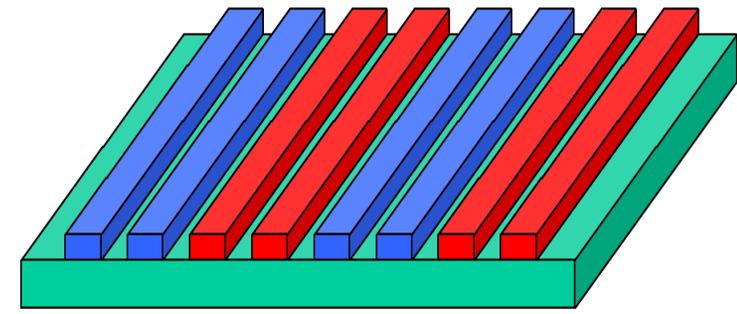


In Tunable add-drop

A. Lupu, H. Benisty, et al., PNFA 2014



Unidirectional DFB laser

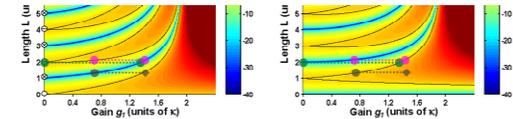


Reconfigurable spatial DMUX

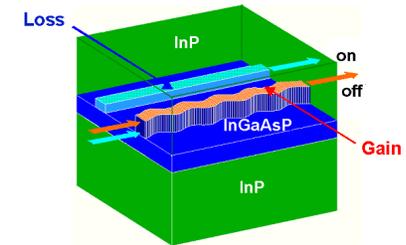
H. Benisty, A. Lupu, A. Degiron, Phys Rev. A 91, 053825 (2015)

Summary and conclusions

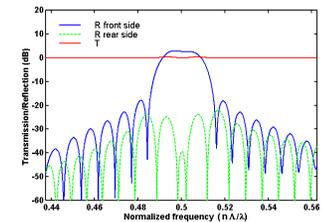
- Perfect Bar and Cross switch states in a non-conservative layout



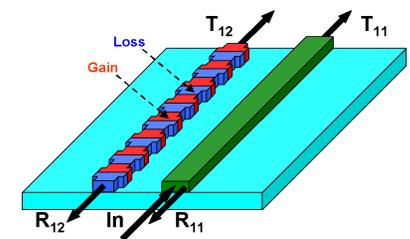
- Impact of material and technological imperfections



- Tailoring spectral properties PT-symmetric Bragg gratings



- Proposal of a new platform for active optical devices





Mind the gap!

Theory

Experiment